

# PEN and Nab: new precision tests of lepton and quark-lepton universality

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This talk will address the question:

In the **LHC era**, can the study of the decays and properties of **light unstable particles**, e.g., **pions**, **muons** and **neutrons** help us to improve our:

- ▶ understanding of the **weak interaction**,
- ▶ understanding of the limits of the **Standard Model**, and
- ▶ searches for any physics that may lie **beyond the SM** ?

Sensitive study topics focus on strong SM principles:

- (a) **quark-lepton universality**,
- (b) **lepton universality**.



# Outline

## The PIBETA & PEN experiments at PSI

The  $\pi^+ \rightarrow \pi^0 e^+ \nu$  ( $\pi_{e3}$ ), pion beta decay

The  $\pi^+ \rightarrow e^+ \nu_e$  ( $\pi_{e2}$ ), electronic decay

The  $\pi^+ \rightarrow e^+ \nu_e \gamma$  ( $\pi_{e2\gamma}$ ), radiative electronic decay

## Neutron decay measurements: Nab and abBA

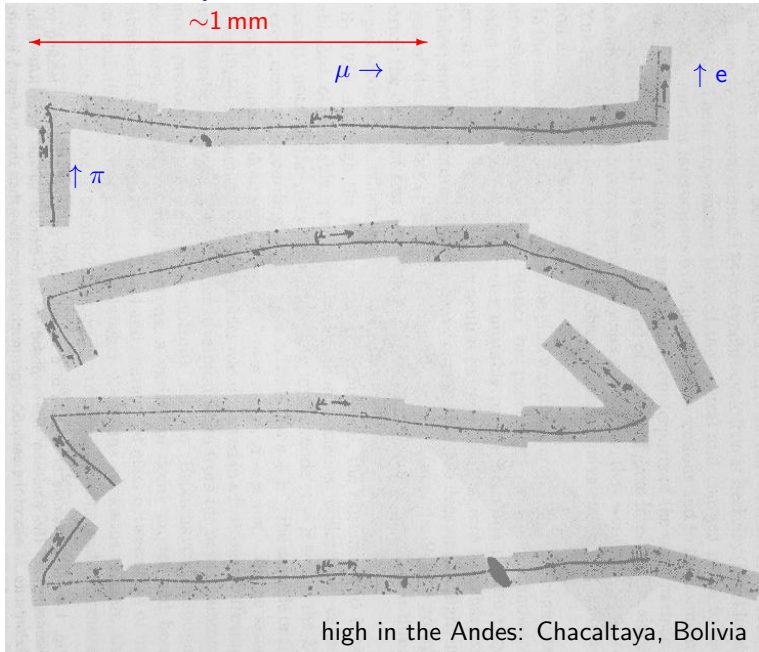
Motivation and goals of Nab/abBA

Nab measurement principles and apparatus

## Summary

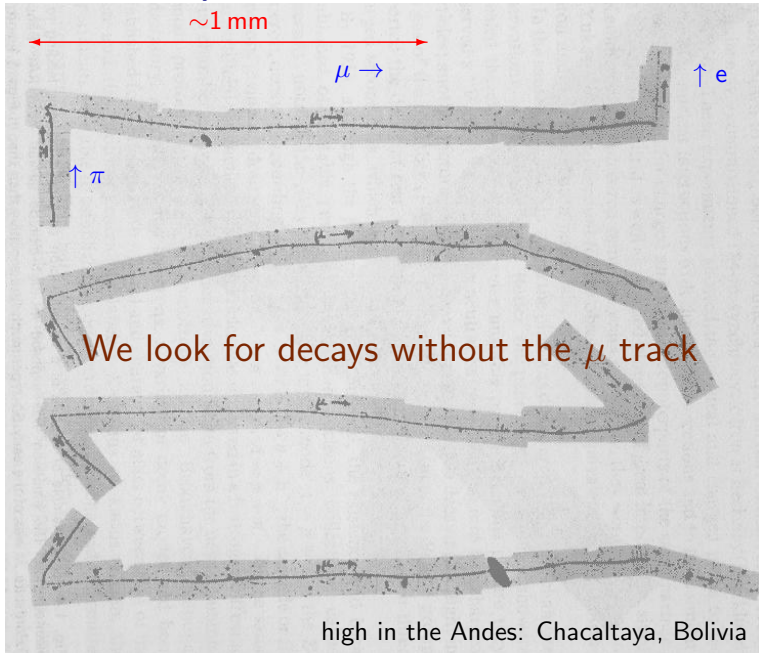


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# Known and measured pion and muon decays

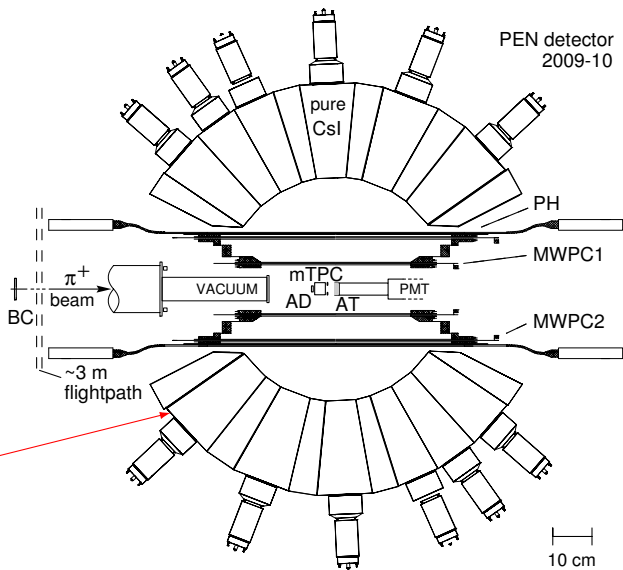
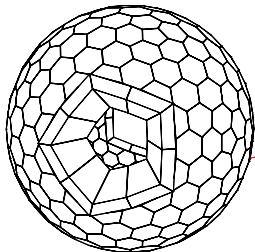
Decay	$BR$	
$\pi^+ \rightarrow \mu^+ \nu$	0.9998770 (4)	$(\pi_{\mu 2})$
$\mu^+ \nu \gamma$	$2.00 (25) \times 10^{-4}$	$(\pi_{\mu 2 \gamma})$
$e^+ \nu$	$1.230 (4) \times 10^{-4}$	$(\pi_{e 2})$
$e^+ \nu \gamma$	$7.39(5) \times 10^{-7}$	$(\pi_{e 2 \gamma})$
$\pi^0 e^+ \nu$	$1.036 (6) \times 10^{-8}$	$(\pi_{e 3}, \pi_{\beta})$
$e^+ \nu e^+ e^-$	$3.2 (5) \times 10^{-9}$	$(\pi_{e 2 ee})$
$\pi^0 \rightarrow \gamma \gamma$	0.98798 (32)	
$e^+ e^- \gamma$	$1.198 (32) \times 10^{-2}$	(Dalitz)
$e^+ e^- e^+ e^-$	$3.14 (30) \times 10^{-5}$	
$e^+ e^-$	$6.2 (5) \times 10^{-8}$	
$\mu^+ \rightarrow e^+ \nu \bar{\nu}$	$\sim 1.0$	(Michel)
$e^+ \nu \bar{\nu} \gamma$	0.014 (4)	(RMD)
$e^+ \nu \bar{\nu} e^+ e^-$	$3.4 (4) \times 10^{-5}$	

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# The PIBETA/PEN apparatus

- $\pi$ E1 beamline at PSI
- stopped  $\pi^+$  beam
- active target counter
- 240-detector, spherical pure CsI calorimeter
- central tracking
- beam tracking
- digitized waveforms
- stable temp./humidity





Pion beta ( $\pi_{e3}$ ) decay:



$$\text{BR} \sim 10^{-8}$$

A theoretically clean path to access CKM  $V_{ud}$



## $\pi_{e3}$ decay: quark-lepton (Cabibbo) universality

The basic weak-interaction **V-A** form (e.g.,  $\mu$  decay):

$$\mathcal{M} \propto \langle e | l^\alpha | \nu_e \rangle \rightarrow \bar{u}_e \gamma^\alpha (1 - \gamma_5) u_\nu$$

is replicated in hadronic weak decays

$$\mathcal{M} \propto \langle p | h^\alpha | n \rangle \rightarrow \bar{u}_p \gamma^\alpha (\mathbf{G}_V - \mathbf{G}_A \gamma_5) u_n \quad \text{with} \quad \mathbf{G}_{V,A} \simeq \mathbf{1} .$$

Departure from  $\mathbf{G}_V = \mathbf{1}$  (**CVC**) comes from **weak quark (Cabibbo) mixing**:  
 $\mathbf{G}_V = \mathbf{G}_\mu \cos \theta_C (= \mathbf{G}_\mu \mathbf{V}_{ud}) \quad \cos \theta_C \simeq 0.97$

3 **q** generations lead to the Cabibbo-Kobayashi-Maskawa (CKM) matrix (1973):

$$\begin{pmatrix} \mathbf{V}_{ud} & \mathbf{V}_{us} & \mathbf{V}_{ub} \\ \mathbf{V}_{cd} & \mathbf{V}_{cs} & \mathbf{V}_{cb} \\ \mathbf{V}_{td} & \mathbf{V}_{ts} & \mathbf{V}_{tb} \end{pmatrix}$$

CKM unitarity cond.:  $\Delta \mathbf{V}^2 = 1 - (|\mathbf{V}_{ud}|^2 + |\mathbf{V}_{us}|^2 + |\mathbf{V}_{ub}|^2) \stackrel{?}{=} 0$ ,  
stringently tests the SM. Until 2004 appeared violated by  $\sim 3\sigma$ !

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where

$$\Delta = m_+ - m_0 = 4.5936(5) \text{ MeV} \quad \text{and} \quad \epsilon = \left(\frac{m_e}{\Delta}\right)^2 \simeq \frac{1}{81}$$

while

$$f(\epsilon, \Delta) = \sqrt{1 - \epsilon} \left(1 - \frac{9}{2}\epsilon - 4\epsilon^2\right) + \frac{\epsilon^2}{4} \ln \left(\frac{1 - \sqrt{1 - \epsilon}}{\sqrt{\epsilon}}\right) - \frac{3}{7} \frac{\Delta^2}{(m_+ + m_0)^2} \simeq 0.941$$

and  $\delta_\pi \sim 0.035$  is the sum of radiative/loop corrections with  $\sim 0.05\%$  relative uncertainty.

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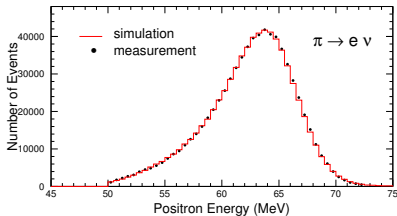
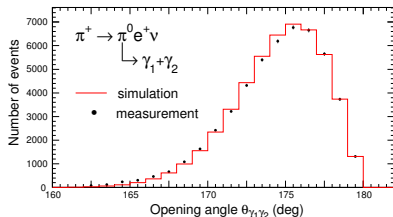
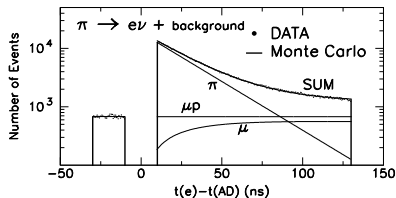
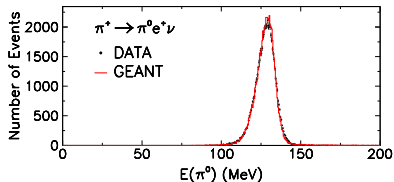
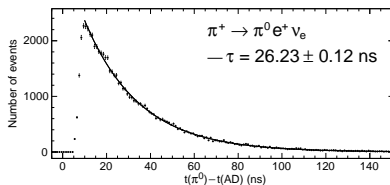
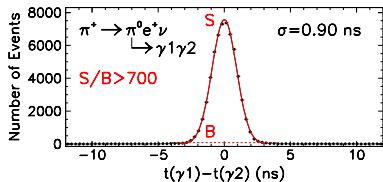
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Prior to 2004,  $\Gamma$  and  $B$  measured with about 4% precision.





## PIBETA result for $\pi^+ \rightarrow \pi^0 e^+ \nu$ ( $\pi_\beta$ ) decay [PRL 93, 181803 (2004)]

Pion beta decay yield normalized to recorded  $\pi \rightarrow e \nu$  events:

$$B_{\pi\beta}^{\text{exp-t}} = [1.040 \pm 0.004 (\text{stat}) \pm 0.004 (\text{syst})] \times 10^{-8},$$

$$B_{\pi\beta}^{\text{exp-e}} = [1.036 \pm 0.004 (\text{stat}) \pm 0.004 (\text{syst}) \pm 0.003 (\pi_{e2})] \times 10^{-8},$$

McFarlane et al. [PRD 1985]:  $B = (1.026 \pm 0.039) \times 10^{-8}$

SM Prediction (PDG):

$$B = 1.038 - 1.041 \times 10^{-8} \quad (90\% \text{ C.L.}) \\ (1.005 - 1.007 \times 10^{-8} \quad \text{excl. rad. corr.})$$

⇒ Most sensitive test of CVC/radiative corr. in a meson to date!

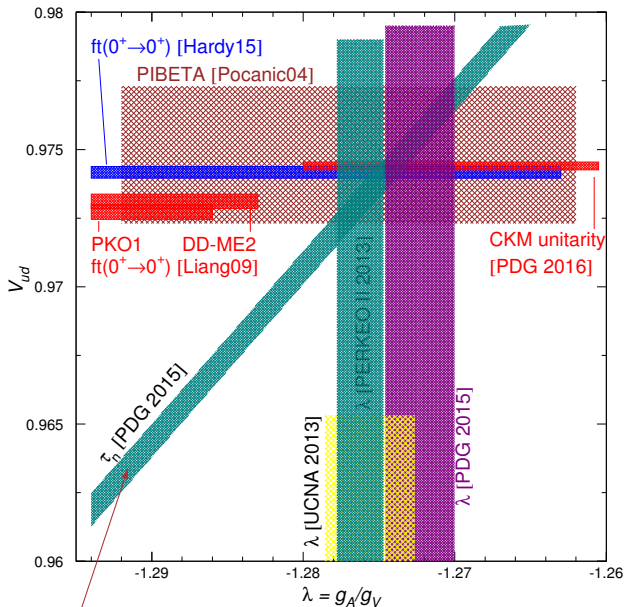
PDG 2016:  $V_{ud} = 0.97417(21)$

PIBETA:  $V_{ud} = 0.9748(25)$  or  $V_{ud} = 0.9728(30)$ .



# Current status of $V_{ud}$ :

Neutron  $\beta$  decay  
results need to be  
sorted out before  
returning to  $\pi_{e3}$ .



$$\tau_n^{-1} \propto |V_{ud}|^2 |g_V|^2 (1 + 3|\lambda|^2)$$

The electronic ( $\pi_{e2}$ ) decay:



$$\text{BR} \sim 10^{-4}$$



## $\pi_{e2}$ decay: SM calculations, lepton universality

- ▶ Early evidence for  $V - A$  nature of weak interaction.

$$R_{e/\mu}^{\pi} = \frac{\Gamma(\pi \rightarrow e\bar{\nu}(\gamma))}{\Gamma(\pi \rightarrow \mu\bar{\nu}(\gamma))} = \frac{g_e^2 m_e^2 (1 - m_e^2/m_{\mu}^2)^2}{g_{\mu}^2 m_{\mu}^2 (1 - m_{\mu}^2/m_{\pi}^2)^2} (1 + \delta R_{e/\mu})$$

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CALC

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**WHY SHOULD WE CARE?**



## Reach of $\pi_{e2}$ decay beyond the SM (New Physics)

$$\mathcal{L}_{\text{NP}} = \left[ \pm \frac{\pi}{2\Lambda_V^2} \bar{u} \gamma_\alpha d \pm \frac{\pi}{2\Lambda_A^2} \bar{u} \gamma_\alpha \gamma_5 d \right] \bar{e} \gamma^\alpha (1 - \gamma_5) \nu$$
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$$\boxed{\Lambda_P \leq 1000 \text{ TeV}} \quad \text{and} \quad \boxed{\Lambda_A \leq 20 \text{ TeV}},$$

and indirectly, through loop effects to  $\boxed{\Lambda_S \leq 60 \text{ TeV}}$ .

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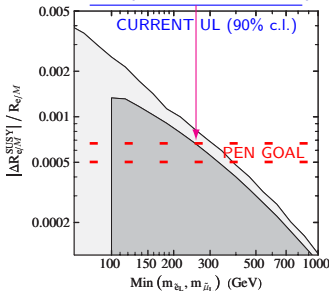
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In general multi-Higgs models with charged-Higgs couplings

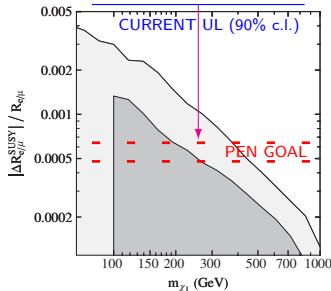
$\lambda_{e\nu} \approx \lambda_{\mu\nu} \approx \lambda_{\tau\nu}$ , at 0.1% precision,  $R_{e\mu}^\pi$  probes  $m_{H^\pm} \leq 400 \text{ GeV}$ .

# MSSM calculations (R parity cons.) [Ramsey-Musolf et al., PR D76 (2007) 095017]

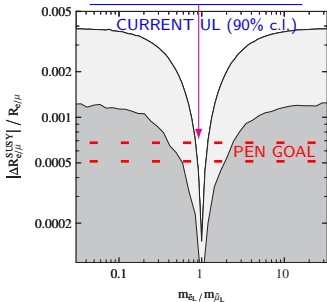
minimal  
selectron,  
smuon  
masses:



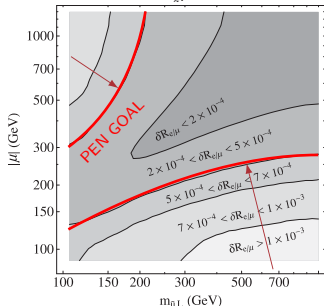
lowest  
mass  
chargino:



slepton  
mass de-  
generacy:



Higgsino  
mass  
param's.  
 $\mu, m_{\tilde{U}_L}$ :

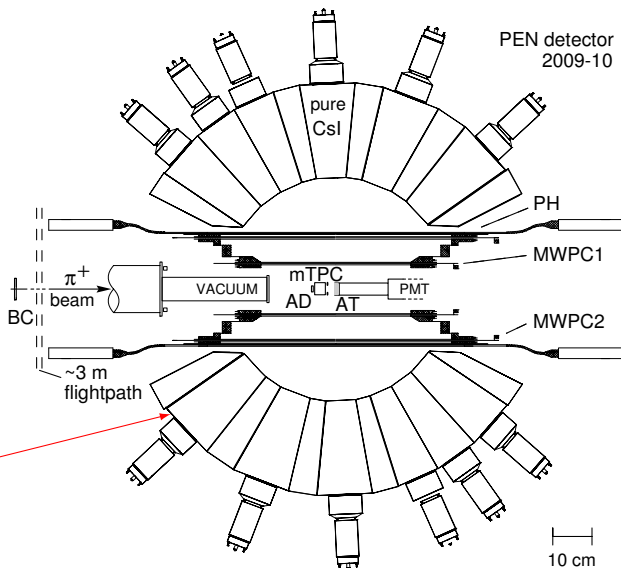
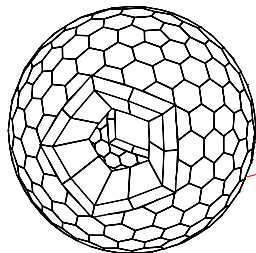


(R parity violating scenario constraints also discussed.)



# The PEN/PIBETA apparatus

- stopped  $\pi^+$  beam
- active target counter
- 240-detector, spherical pure CsI calorimeter
- central tracking
- beam tracking
- digitized waveforms
- stable temp./humidity



# The PEN/PIBETA apparatus

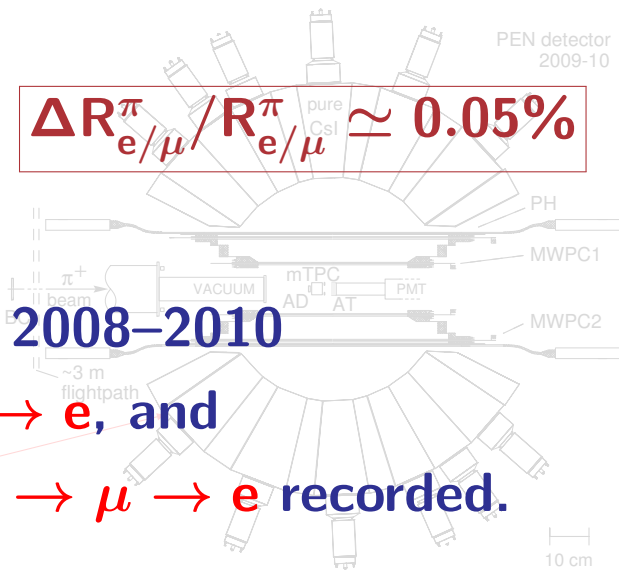
- stopped  $\pi^+$  beam
- active target counter
- 20 detector spherical pure CsI calorimeter
- central tracking
- beam tracking
- digitized waveforms
- stable temp./humidity

**PEN runs: 2008–2010**

**> 22M  $\pi \rightarrow e$ , and**

**> 200M  $\pi \rightarrow \mu \rightarrow e$  recorded.**

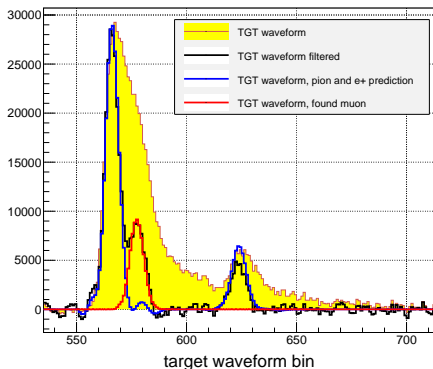
$$\Delta R_{e/\mu}^{\pi} / R_{e/\mu}^{\pi} \approx 0.05\%$$



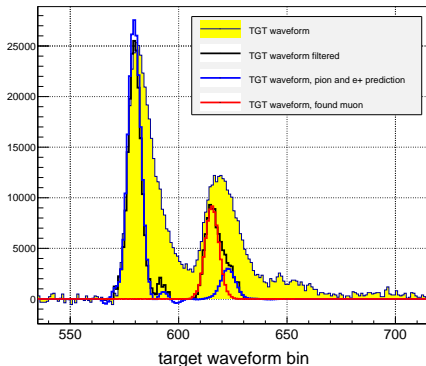
# Highlights and challenges of PEN analysis (under way)

Active target waveforms: separating the decay particle pulses!

Early pion decay (extremely common)

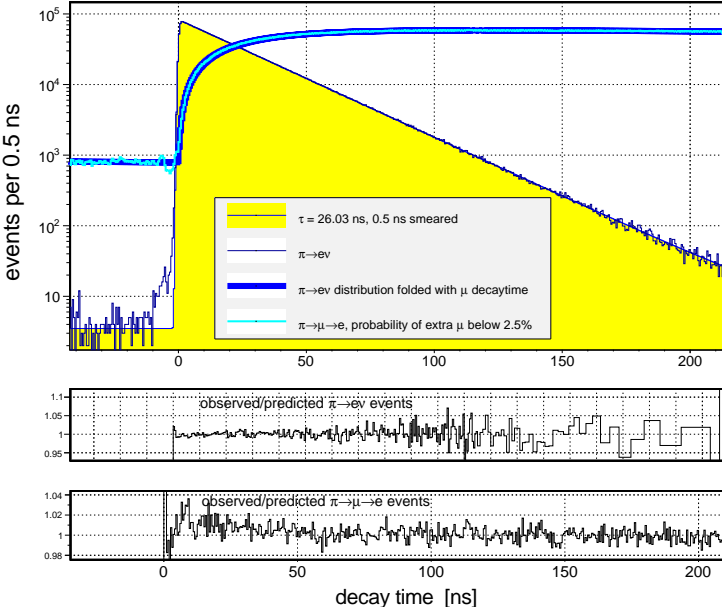


Early muon decay (still annoying)



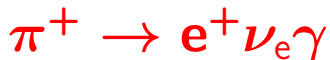
- ▶  $\pi$  and  $e^+$  pulse time and amplitude predicted from other detector systems (mTPC, MWPCs, PH)!
- ▶ Waveform system functions evaluated based on prompt hadronic events.
- ▶ Hypotheses with/without a  $\mu$  pulse evaluated.

# PEN: agreement with predictions (2010 data analysis)





Radiative electronic ( $\pi_{e2\gamma}$ ) decay:



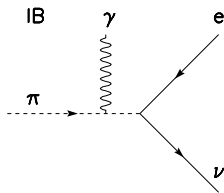
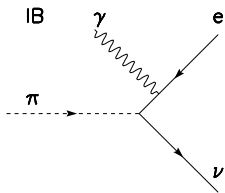
$$\text{BR}_{\text{non-IB}} \sim 10^{-7}$$



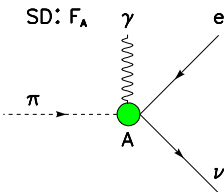
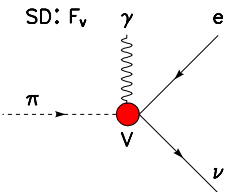
# Physics of

$\pi^+ \rightarrow e^+ \nu \gamma$  (RPD):

QED IB terms:

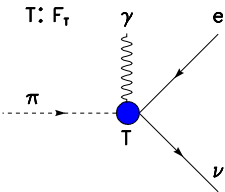


and SD  $V$ ,  $A$  terms:



SM

A tensor interaction,  
too?



Exchange of  $S=0$  leptoquarks

P Herczeg, PRD 49 (1994) 247



## The $\pi \rightarrow e\nu\gamma$ amplitude and FF's

The IB amplitude (QED **uninteresting!**):

$$M_{\text{IB}} = -i \frac{eG_F V_{ud}}{\sqrt{2}} f_\pi m_e \epsilon^{\mu*} \bar{e} \left( \frac{k_\mu}{kq} - \frac{p_\mu}{pq} + \frac{\sigma_{\mu\nu} q^\nu}{2kq} \right) \times (1 - \gamma_5) \nu.$$

The structure-dependent amplitude (**interesting!**):

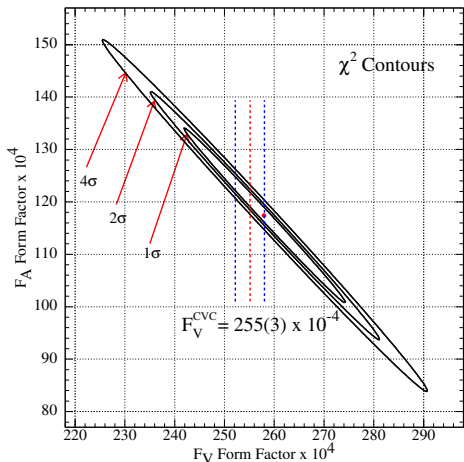
$$M_{\text{SD}} = \frac{eG_F V_{ud}}{m_\pi \sqrt{2}} \epsilon^{\nu*} \bar{e} \gamma^\mu (1 - \gamma_5) \nu \times [F_V \epsilon_{\mu\nu\sigma\tau} p^\sigma q^\tau + iF_A (g_{\mu\nu} pq - p_\nu q_\mu)].$$

The SM branching ratio ( $x = 2E_\gamma/m_\pi$ ;  $y = 2E_e/m_\pi$ ),

$$\begin{aligned} \frac{d\Gamma_{\pi e 2\gamma}}{dx dy} = & \frac{\alpha}{2\pi} \Gamma_{\pi e 2} \left\{ IB(x, y) + \left( \frac{m_\pi^2}{2f_\pi m_e} \right)^2 \right. \\ & \times [(F_V + F_A)^2 \text{SD}^+(x, y) + (F_V - F_A)^2 \text{SD}^-(x, y)] \\ & \left. + \frac{m_\pi}{f_\pi} [(F_V + F_A) S_{\text{int}}^+(x, y) + (F_V - F_A) S_{\text{int}}^-(x, y)] \right\}. \end{aligned}$$

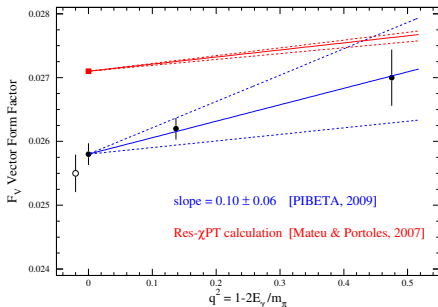
# PIBETA results for $\pi \rightarrow e\nu\gamma$

Best values of pion Form Factor Parameters:



Combined analysis of 1999-01 and 2004 data sets

[Bychkov et al., PRL **103**, 051802 (2009)]



# Summary of PIBETA results on $\pi \rightarrow e\nu\gamma$ [PRL **103**, 051802 (2009)]

$$\mathbf{F_V = 0.0258 \pm 0.0017} \quad (\mathbf{8\times})$$

$$\mathbf{F_A = 0.0119 \pm 0.0001}^{\text{exp}}_{(\text{F}_V^{\text{CVC}})} \quad (\mathbf{16\times})$$

$$\mathbf{a = 0.10 \pm 0.06} \quad (\mathbf{q^2 \text{ dep of } F_V}) \quad (\mathbf{\infty})$$

$$\mathbf{-5.2 \times 10^{-4} < F_T < 4.0 \times 10^{-4}} \quad \mathbf{90\% \text{ C.L.}}$$

$$\mathbf{B_{\pi_{e2\gamma}}(E_\gamma > 10 \text{ MeV}, \theta_{e\gamma} > 40^\circ) = 73.86(54) \times 10^{-8}} \quad (\mathbf{17\times})$$



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Above results will be improved with the new PEN data analysis.

At L.O. ( $I_9 + I_{10}$ ),  $F_A$ ,  $F_V$  are related to pion polarizability and  $\pi^0$  lifetime

$$\alpha_E^{\text{LO}} = -\beta_M^{\text{LO}} = (2.783 \pm 0.023_{\text{exp}}) \times 10^{-4} \text{ fm}^3$$

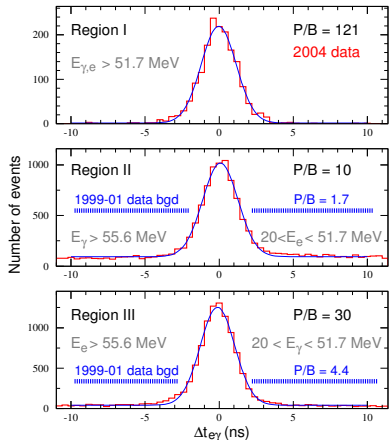
$$\tau_{\pi^0} = (8.5 \pm 1.1) \times 10^{-17} \text{ s} \quad \left\{ \begin{array}{l} \text{current PDG avg: } 8.52(12) \\ \text{PrimEx PRL '10: } 8.32(23) \end{array} \right.$$



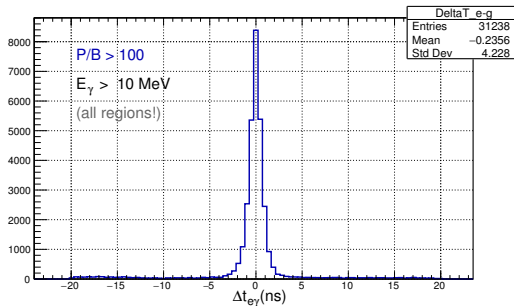
# How PEN data will improve $\pi \rightarrow e\nu\gamma$ analysis

We compare accidental coincidence rates in 3 generations of data:

## PIBETA data



## Current PEN data





# Neutron beta decay program SNS (NIST)



## Neutron beta decay observables (SM)

$$\frac{dw}{dE_e d\Omega_e d\Omega_\nu} \simeq p_e E_e (E_0 - E_e)^2 \times \left[ 1 + a \frac{\vec{p}_e \cdot \vec{p}_\nu}{E_e E_\nu} + b \frac{m}{E_e} + \langle \vec{\sigma}_n \rangle \cdot \left( A \frac{\vec{p}_e}{E_e} + B \frac{\vec{p}_\nu}{E_\nu} \right) + \dots \right]$$

where in SM:

$$a = \frac{1 - |\lambda|^2}{1 + 3|\lambda|^2} \quad A = -2 \frac{|\lambda|^2 + \text{Re}(\lambda)}{1 + 3|\lambda|^2}$$

$$B = 2 \frac{|\lambda|^2 - \text{Re}(\lambda)}{1 + 3|\lambda|^2} \quad \lambda = \frac{G_A}{G_V} \text{ (with } \tau_n \Rightarrow \text{CKM } V_{ud}\text{)}$$

also proton asymmetry:  $C = \kappa(A + B)$  where  $\kappa \simeq 0.275$ .

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also proton asymmetry:  $C = \kappa(A + B)$  where  $\kappa \simeq 0.275$ .

⇒ SM overconstrains  $a$ ,  $A$ ,  $B$  observables in  $n$   $\beta$  decay!  
Fierz interf. term  $b$  brings add'l. sensitivity to non-SM processes!

# Goals of the Nab experiment (at SNS, ORNL)

- ▶ Measure the  $e-\nu$  correlation  $a$  in neutron decay with precision

$\Delta a/a \simeq 10^{-3}$  or  $\sim 50\times$  better than:

	$-0.1054 \pm 0.0055$	Byrne et al '02
current results:	$-0.1017 \pm 0.0051$	Stratowa et al '78
	$-0.091 \pm 0.039$	Grigorev et al '68



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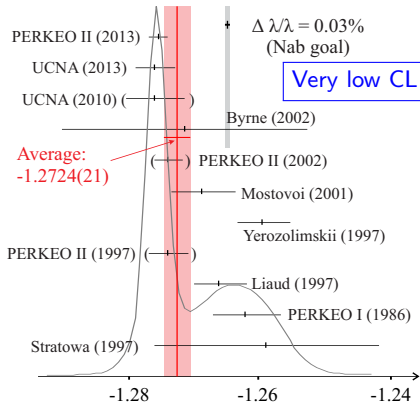
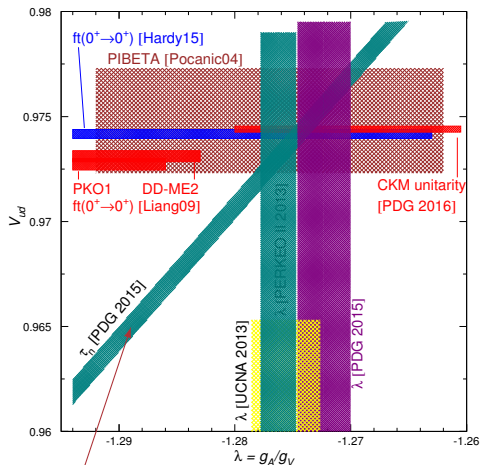
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## Motivation:

- multiple independent determinations of  $\lambda$  (test of CKM unitarity),
- independent and competitive limits on  $S$ ,  $T$  currents (BSM).

# Current status of $V_{ud}$ and $\lambda$ , from $n$ decay

... remains an unresolved mess:



Very low CL!

Average:  
-1.2724(21)

$$\frac{\Delta \lambda}{\lambda} \simeq 0.27 \frac{\Delta a}{a} \simeq 0.24 \frac{\Delta A}{A}$$

$\lambda$  sensitivity to  $a$ ,  $A$  is similar.

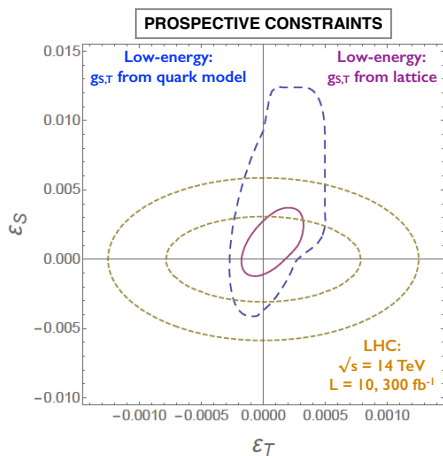
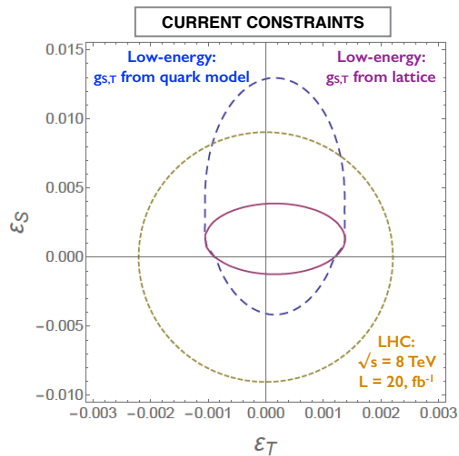
$$\tau_n^{-1} \propto |V_{ud}|^2 |g_V|^2 (1 + 3|\lambda|^2)$$

- ▶ Nab+abBA  $\Rightarrow$  several independent  $\sim 0.03\%$  determinations of  $\lambda$ ,
- ▶ Combined with  $b \Rightarrow$  new limits on non-SM terms, esp. Tensor.





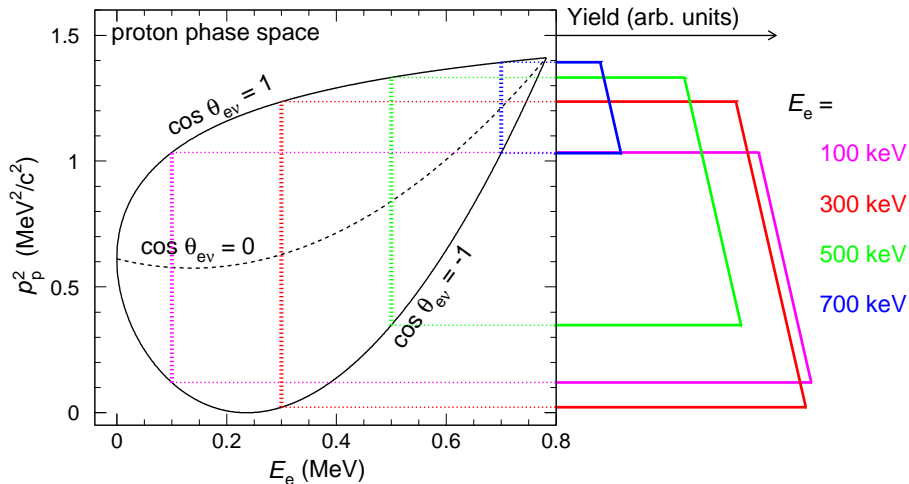
# Limits on $T$ , $S$ couplings from beta decay



Measurement of  $b$  with  $\delta b < 10^{-3} \Rightarrow > 4\text{-fold improvement}$  on the current limit for  $\epsilon_T$  from  $\pi^+ \rightarrow e^+ \nu \gamma$  decay.

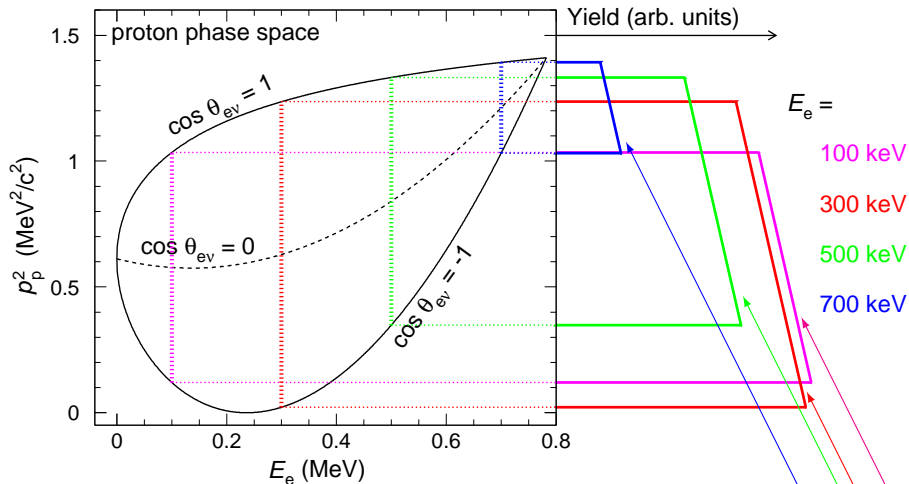
From Bhattacharya, Cirigliano, et al., PRD **94** (2016) 054508 [arXiv 1606.07049].

# Nab measurement principles: proton phase space



NB: For a given  $E_e$ ,  $\cos \theta_{ev}$  is a function of  $p_p^2$  only.

# Nab measurement principles: proton phase space



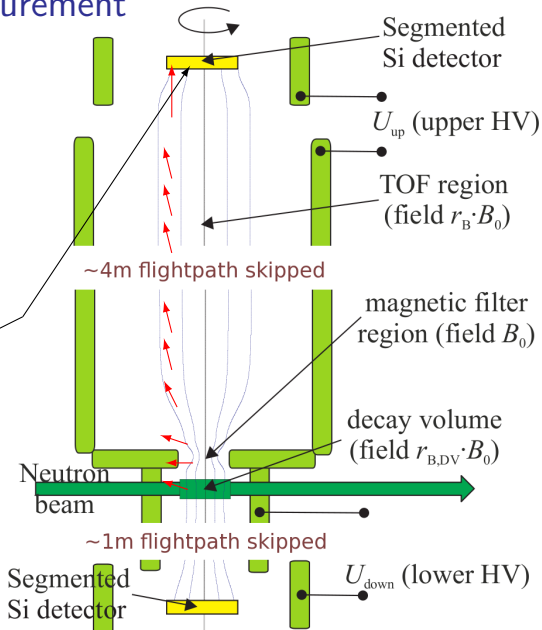
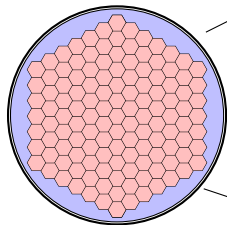
NB: For a given  $E_e$ ,  $\cos \theta_{ev}$  is a function of  $p_p^2$  only.

Slope  $\propto a$

**Numerous consistency checks are built-in!**

# Nab principles of measurement

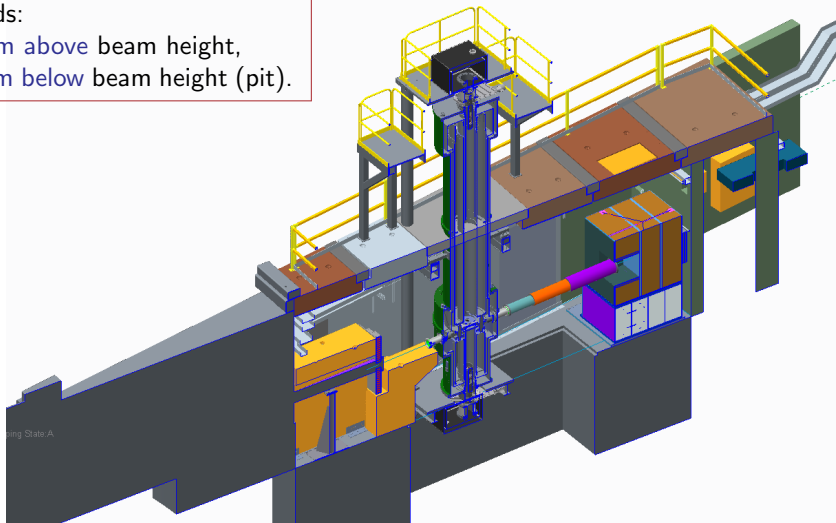
- ▶ Collect and detect both **electron** and **proton** from neutron beta decay.
- ▶ Measure  $E_e$  and  $TOF_p$  and reconstruct decay kinematics
- ▶ Segmented Si det's:



# Nab apparatus in FnPB

extends:

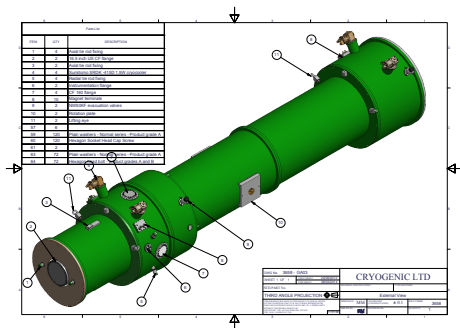
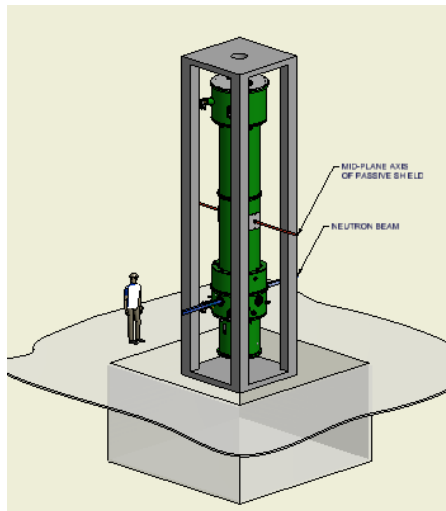
- $\sim 6$  m above beam height,
- $\sim 2$  m below beam height (pit).



Designed to measure **a**, **b** with:

$$\frac{\Delta a}{a} \simeq 10^{-3} \text{ and } \Delta b \simeq 3 \times 10^{-3}.$$

# Some images of the Nab apparatus



# Precision study of $\pi$ and $n$ decays in PEN and Nab

- ▶ A **significant experimental effort** is under way (in PEN, Nab, and in other experiments) to make use of the **unparalleled theoretical precision** in the weak interactions of the lightest particles.
- ▶ Information obtained is **complementary** to **collider results**, and important for the proper interpretation of the latter.
- ▶ **Significant improvements in precision** for BSM limits stemming from tests of lepton- and quark-lepton universality are forthcoming in the near future.
- ▶ Decision on future measurement of  $\pi^+ \rightarrow \pi^0 e^+ \nu$  will await results of current neutron beta decay experiments.

Home pages: <http://pen.phys.virginia.edu>  
<http://nab.phys.virginia.edu>  
<http://pibeta.phys.virginia.edu>



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<sup>†</sup> **Co-spokesmen**

<sup>\*</sup> **Project Manager**

<sup>‡</sup> **On-site Manager**

<sup>§</sup> **Current students**

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