

Case studies: collider design

by Dream Team

Task statement

Parameter	Ring 1	Ring 2
Ring circumference, m	300	?
Ions	Protons	Deuterons
Energy, GeV/u		3-10
Luminosity		1E+30
	Proton-deuteron collisions	

How we were figured about

Magnetic field is 1.8 T, deuteron ring circumference is 600 m

	p	d
Bending radius, ρ (m)	18.53	37.06
Magnets number	40	40
Dipole percentage	0.3	0.3
Angle of one magnet (degree)	7.	7.
Magnet length (m)	2.26	4.52
Circumference	300	600
β	1.	1.
f_0 (MHz)	1.	0.5

Main intense beam effects

In case of space charge we observe the classical Laslett formula:

$$\Delta q = -\frac{Z^2}{A} \frac{Nr_i}{4\pi\beta^2\gamma^3\varepsilon} k_{bunch} \quad k_{bunch} = \frac{c_{ring}}{\sqrt{2\pi}\sigma_s}$$

Beam – beam effect:

$$\xi_{12} = -\frac{Z_1 Z_2}{A_2} \frac{N_2 r_i (1 + \beta_1 \beta_2)}{2\pi\beta_1^2\gamma_1\varepsilon} \Phi_{12} \lambda_0 \quad \text{when emittances, beta-functions, longitudinal lengths are equals}$$

$$\Phi_{12} = \frac{1}{\sqrt{2\pi}} \int_{-\infty}^{\infty} \frac{1}{\sqrt{1 + (\alpha u)^2}} e^{-2u^2} du \quad \Phi_{12} = 0.913, \text{ when } \sigma_s = \beta^*$$

It is known from practice that an intense beam is stable if $|\xi| + |\Delta q| \leq 0.05$

In this case we can increase amount of the particles and emittance, we have

$$L \sim \frac{N_1 N_2}{\varepsilon} \sim \varepsilon$$

Intersection point

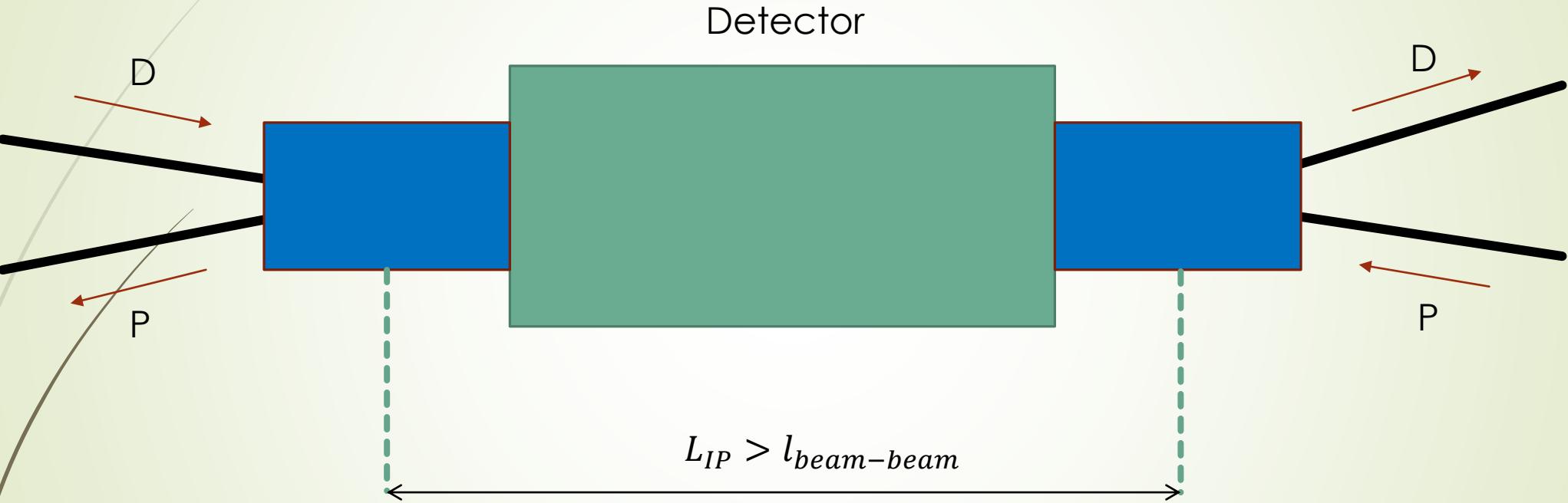
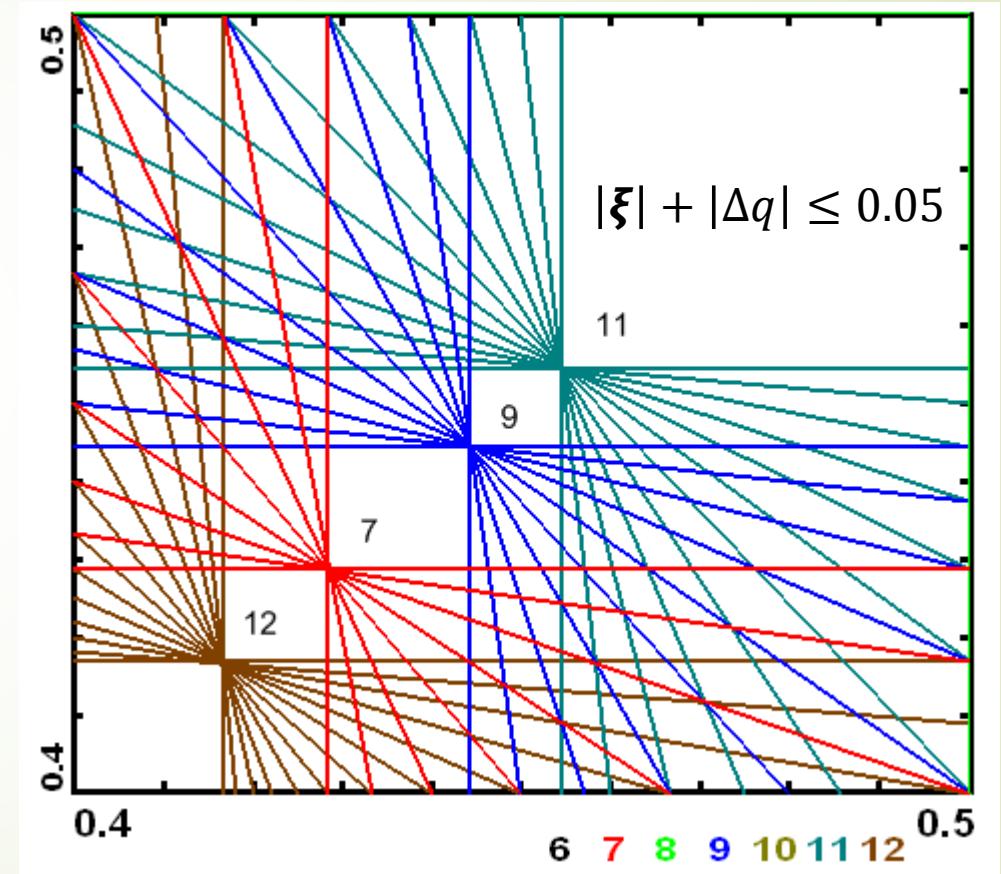
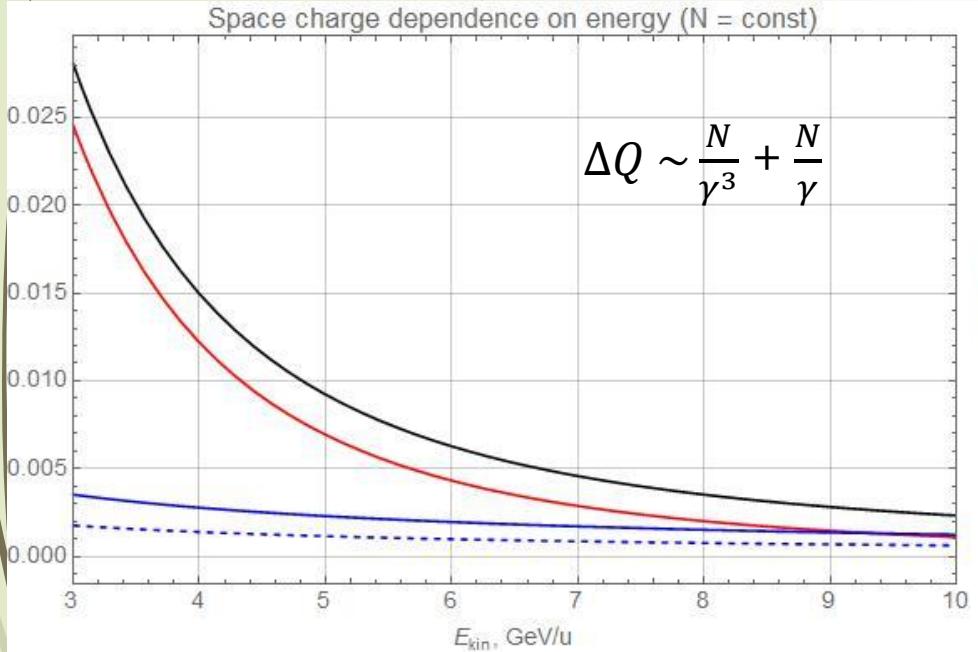


Table of parameters

Parameter	Value
Kinetic energy, GeV/u	3
$\sigma_s = \beta^*, m$	0.5
H, harmonic number	100 (p), 200 (d)
N beam	25 (p), 50 (d)
Emittance, mm*mrad	1
Particles per bunch	6E+10
ξ_{12}	0.0033
Δq (Laslett)	0.0245
$ \xi + \Delta q $	0.0278
Luminosity	1.09E+30

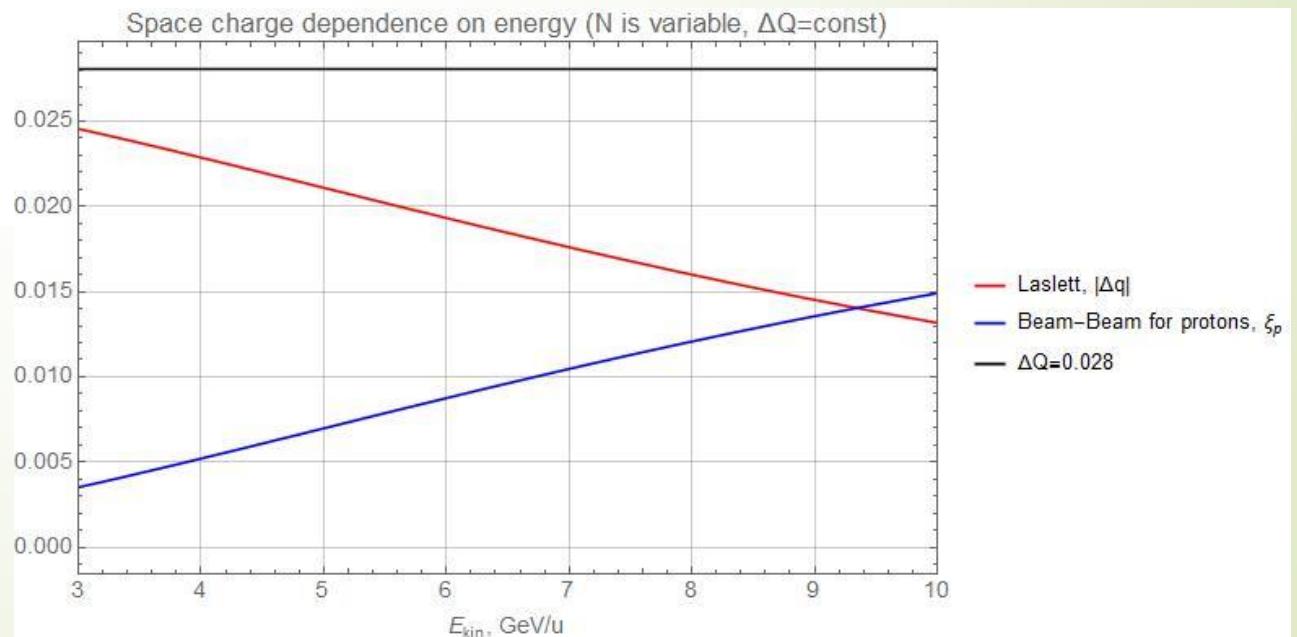
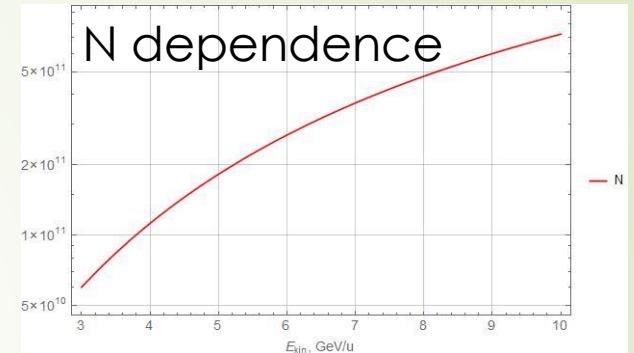


Space charge and beam-beam



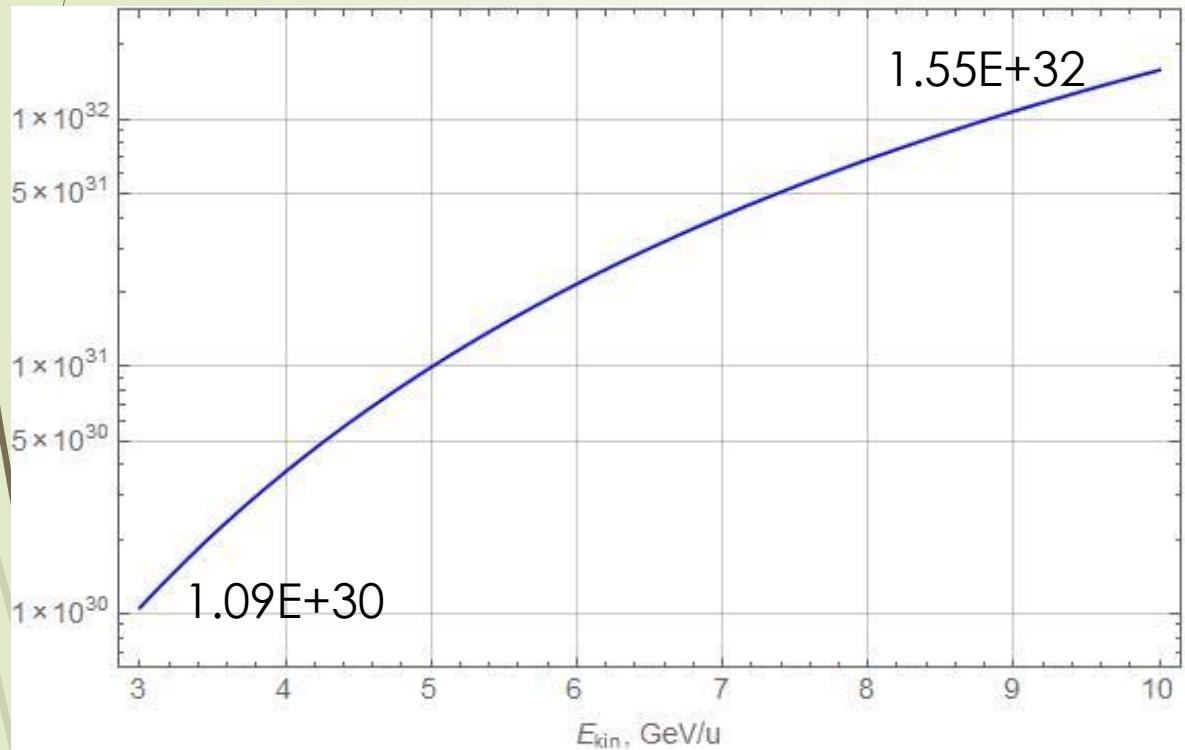
$$\Delta q = -\frac{Z^2}{A} \frac{Nr_i}{4\pi\beta^2\gamma^3\varepsilon} k_{\text{bunch}}$$

- Laslett, $|\Delta q|$
- Beam-Beam for protons, ξ
- - - Beam-Beam for deuterons
- $\Delta Q = |\Delta q| + |\xi|$



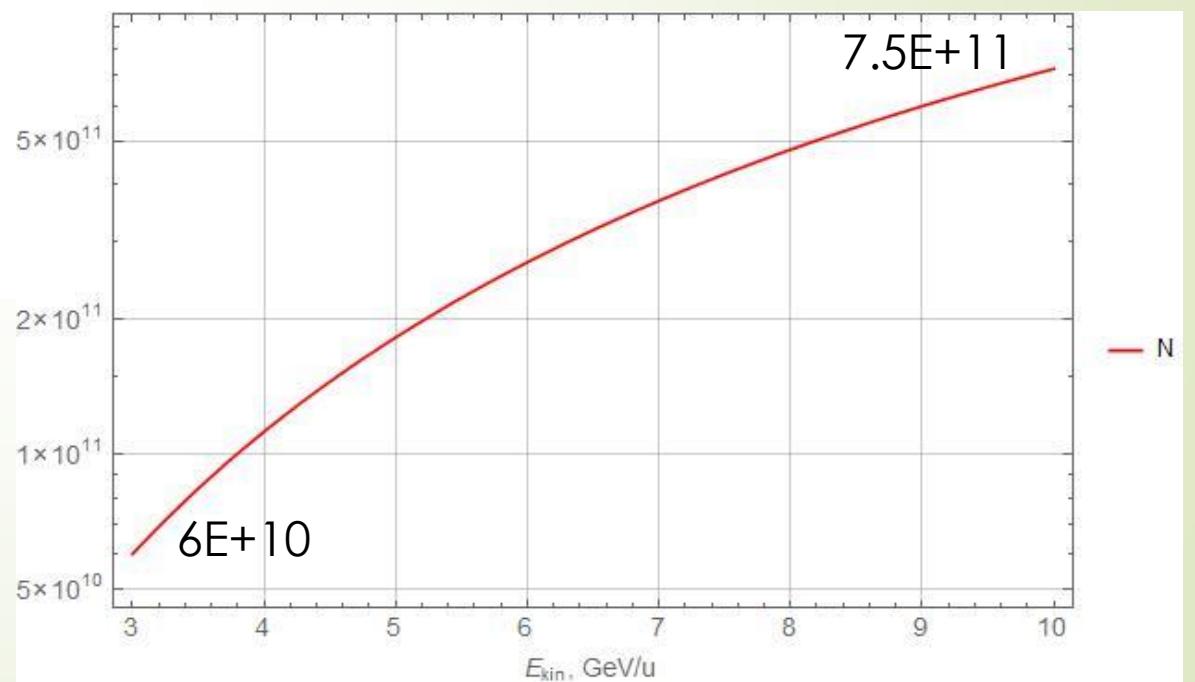
$$\xi_{12} = -\frac{Z_1 Z_2}{A_2} \frac{N_2 r_i (1 + \beta_1 \beta_2)}{2\pi\beta_1^2 \gamma_1 \varepsilon} \Phi_{12} \lambda_0$$

Luminosity and particles number

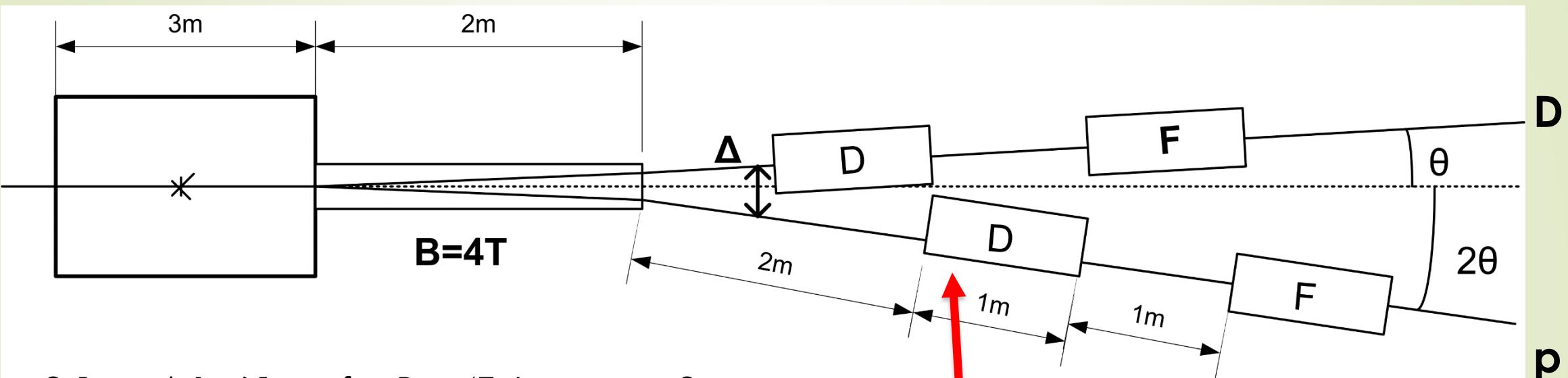


$$L = \frac{N_{\text{bunches}} N_p N_d f_0}{4\pi \epsilon \beta^*} \Phi_{hg}$$

$\Phi_{hg} = 0.7578$
If $\sigma_s = \beta^*$



Final Focusing Estimation ($E_{\text{kin}} = 10 \text{ GeV/u}$)



$\theta=0.1$ and $\Delta=61\text{cm}$ for $B = 4\text{T}$, $L_{\text{magn}} = 2\text{m}$

$$F_{\text{doublet}} = \frac{L_{\text{full}}}{2} \quad (\text{where } L=550 \text{ cm}) \quad \beta^* = 0.5\text{m} \rightarrow \beta_{\max} = 61\text{m} \rightarrow \sigma_{\max} \approx 0.8\text{cm}$$

$$f \approx \sqrt{F_{\text{doublet}} * L_{\text{doublet}}}$$

$$a = \frac{6\sigma_{\max}}{2} = 2.3\text{cm} - \text{aperture radius}$$

$$G = \frac{1}{300} \frac{pc}{e} \frac{1}{fl}$$

G ≈ 4.6 kG/cm

$$J = \frac{ca^2}{8\pi} G$$

J ≈ 9 kA

Dreams about lattice (for $E_{\text{kin}}=3 \text{ GeV}$)

	k, m^{-2}	G, kG
Final Focusing: dublet		
F	0,6	0,82
D	-0,6	-0,82
FODO		
F	0,825	1,1
D	-0,745	-1,0

