

JAS 2019 – Ion Colliders

Heavy-lons in the LHC

by

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With big acknowledgements to John Jowett

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Introduction

- History and Notations
- Effects on Luminosity

Pb-Pb Collisions

- Secondary Beams
- Getting the beams into LHC
- Beam and Luminosity Evolution
- Performance Summary

Other Operational Modes

- p-Pb collisions
- Other unforeseen, but successful operational modes

Introduction to LHC

The largest machine in the world: The Large Hadron Collider (LHC)





27 km circumference100m underground

Accelerates protons and heavy-ions to E = 6.5 Z TeV (2018).

Collides 2 counter-rotating beams in 4 physics experiments.

Collision Modes in LHC

p-p



The LHC spends most of its time colliding **proton-proton (p-p)** in its 4 main experiments.

All are also highly capable heavy-ion experiments: ALICE (IP2) and ATLAS (IP1) / CMS (IP5) LHCb (IP8) since 2012 also LHCf (cosmic ray physics)

1 month/year colliding **fully stripped lead** (²⁰⁸Pb⁸²⁺) or Pb ions with protons.

A short History and Future ...

12 one-month heavy-ion runs between 2010 and 2030. 6/12 done.





Energy of ions/nuclei and nucleons





Energy and momentum are related via the square of the 4-momentum vector, $\mathbf{P} = (E/c, \mathbf{p})$:



Operate at same beam rigidity for different species \rightarrow equivalent beam energy:

$$E_{ion} = E_p Z$$

At high energy E >> mc²

Keep similar magnetic cycles for proton and heavy-ion operation.

$$E \approx pc = 7.0 Z \text{ TeV} = 2.76 A \text{ TeV} = 574 \text{ TeV}$$

Energy per charge,
relation to proton energy
Energy per nucleon
Energy of the particle

Centre-of-Mass Energy

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Centre-of-Mass (CMS) energy is available for the production of new particles.

 $P_{1} = \begin{pmatrix} E_{1}/c \\ \vec{p_{1}} \end{pmatrix} \qquad P_{2} = \begin{pmatrix} E_{2}/c \\ \vec{p_{2}} \end{pmatrix}$

$$E = E_{beam1} + E_{beam2}$$

From the sum of the 4-momentum vectors the **centre-of-mass energy in collision of two different species** can be calculated:

$$\sqrt{(P_1 + P_2)^2} = \sqrt{s} \approx 2p_p \sqrt{Z_1 Z_2}$$

Centre-of-mass energy **per colliding nucleon pair**:

$$\sqrt{s_{NN}} \approx 2p_p \sqrt{\frac{Z_1 Z_2}{A_1 A_2}}$$

proton momentum

LHC Pb-Pb run in 2015/18:

$$\sqrt{s} = 2 \times 6.37 \times 82 \text{ TeV} > 1 \text{ PeV}$$
$$\sqrt{s_{NN}} = 2 \times 6.37 \times \frac{82}{208} \text{ TeV} = 5.02 \text{ TeV}$$

New energy frontier in nucleus-nucleus collisions. Continues beyond RHIC ($\sqrt{s_{NN}} = 0.2 \text{ TeV}$) and previous fixed target experiments.

Choice of Beam Energy

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particle charge

Max. beam energy achieved in p-p collisions: $E_b = 6.5 Z$ TeV.

For Pb-Pb, **beam energy** reduction to $E_b = 6.37$ Z TeV.

 \rightarrow Allows comparison of 3 collision modes at the same center-of-mass energy $\sqrt{s_{NN}}$



A particle bunch is characterised by its **number of particles**, $N_b(t)$, and the **normalised** emittances, $\epsilon_{n,i}(t)$, in the three planes (i = x, y, s).

The transverse emittances relate to the beam sizes σ_{xy} :

$$\sigma_{xy}^2 = \epsilon_{xy} \beta_{xy}$$

The beam size shrinks during acceleration by adiabatic damping. Therefore we define the so-called **normalised emittance** ϵ_n , which is constant with energy:

$$\epsilon_{n,xy} = \epsilon_{xy}\sqrt{\gamma^2 - 1} \approx \epsilon_{xy}\gamma$$

Normalized emittance in LHC (γ @7 Z TeV, same beam size) $\epsilon_{n,p} = 3.75 \,\mu\text{m}$ $\gamma_p = 7461$ $\epsilon_{n,Pb} = 1.5 \,\mu\text{m}$ $\gamma_{Pb} = 2963.5$ The rel. Lorentz factor is related to the energy as $E=\gamma mc^2$

Thus, for particles in the same magnetic field

$$\gamma_{ion} = Z \frac{m_p}{m_{ion}} \gamma_p$$

Heavy-lon vs. Proton Operation

- Some similarities with protons: aperture, optics, orbits
 → Bending ∝ Charge (q = Ze): Bρ = p/q
- Charge per ion bunch ~10% of proton bunch:

 \rightarrow collective effects driven by impedance or beam-beam are weak

- Higher charge and mass: Beam dynamics and performance limits of heavy ions are quite different from those of protons.
- Many beam dynamic effects are proportional to high powers of Z. In same accelerator:
 - \rightarrow Strong Intra-beam scattering (IBS) $\alpha Z^3/A^2$.
 - \rightarrow Radiation damping $\alpha Z^5/A^4$.
 - \rightarrow Large event cross-sections for electromagnetic processes.

 \Rightarrow Fast intensity decay and **short luminosity lifetimes**.

 \Rightarrow Secondary beams emerging from the interaction point (IP).

Dominant Effects on Emittance

Intra-Beam Scattering (IBS)

Multiple small-angle Coulomb scattering among charged particles inside their bunch.

Emittance Growth and Particle Losses

Growth rate dynamically changing with beam properties:

$$\alpha_{\rm IBS} \propto \frac{1}{\gamma} \frac{N_b}{\epsilon_{n,x} \epsilon_{n,y} \epsilon_s}$$

Dominating effect in the LHC. Tends to reduce luminosity.

Radiation Damping

Energy loss due to synchrotron radiation emitted by charged particles bent on a circular orbit.

Emittance Shrinkage

Damping rate is **constant** for a given beam energy:

 $\alpha_{\rm rad} \propto \gamma^3$

Starts to become noticeable at LHC energies (and above). Tends to increase luminosity

IBS and radiation damping both depend on particle type.



Luminosity is a measure of the ability of a particle accelerator to produce the required number of interactions:



For *k*_{*b*} **colliding bunches**, which are equal and round:



$$F(\theta_c) = 1/\sqrt{1 + \left(\frac{\theta_c \sigma_z}{2}\right)^2 \frac{\gamma}{\epsilon_n \beta^*}}$$

Depends on machine settings (crossing-angle θ_c , β -function at IP) and beam parameters (emittance ϵ_n , bunch length σ_z)



Machine parameters θ_c, β^* are individually set for the requirements of each experiments.

Number of colliding bunches k_b per IP depends on filling pattern.

LHC Heavy-Ion runs are complicated!

4 experiments with sometimes very different requests and conditions, luminosity sharing, ...

Nucleon-Nucleon Luminosity

The nucleus-nucleus luminosities for collisions of different species or asymmetric collisions (e.g. p-Pb) are very different and may seem low compared to p-p.

In order to make a meaningful comparison one has to look at the **nucleon-nucleon luminosity**:

$$\mathcal{L} = 1.0 \times 10^{27} \text{cm}^{-2} \text{s}^{-1} \text{ (Pb - Pb)} = 4.3 \times 10^{31} \text{cm}^{-2} \text{s}^{-1} \text{ (nucleon - nucleon)}$$

Interaction Cross-sections

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Bound-free pair production (BFPP)

 208 Pb⁸²⁺ + 208 Pb⁸²⁺ \rightarrow^{208} Pb⁸²⁺ + 208 Pb⁸¹⁺ + e⁺



These **ultraperipheral interactions** have large interaction cross-sections in Pb-Pb collisions and are the main contribution to **fast luminosity burn-off** and **short beam lifetime**:

Event rate:
$$\frac{dR}{dt} = -\frac{dN}{dt} = \sigma_c \mathcal{L}$$

Electromagnetic dissociation (EMD)

 $\label{eq:208} {\rm Pb}^{82+} + {\rm ^{208}\ Pb}^{82+} \rightarrow {\rm ^{208}\ Pb}^{82+} + {\rm ^{207}\ Pb}^{82+} + n$...and higher orders



$$\sigma_{c,tot} = \sigma_{BFPP} + \sigma_{EMD} + \sigma_{hadron}$$

$$\approx 281 \text{ b} + 226 \text{ b} + 8 \text{ b}$$

$$= 515 \text{ b} \qquad \text{@ 7 Z TeV}$$



Secondary Beams Created in the Collision

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These reactions change the charge-to-mass ratio of the ions, which changes bending in (main) dipoles: $B\rho = p/q$

Secondary Beam Paths right of IP5 Secondary beams with 0.03 Main: 208-Pb-82+ rigidity change 0.02 $B\rho(1+\delta)$ BFPP: 208-Pb-81+ BFPP1 EMD1 0.01 EMD: 207-Pb-82+ where x [m] 0.00 $\delta = \frac{1 + \Delta m / m_{Pb}}{1 + \Delta O / O} - 1$ -0.01**Intense secondary** -0.02beams are produced -0.03that impact in a 100 200 300 400 500 0 Luminosity limit, s [m from IP5] superconducting if deposited power BFPP1 magnet downstream exceeds quench limit. main beam from the IP. EMD1

Loss Pattern around the Ring

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Direct limit of luminosity

Beam loss spikes around all IPs where ions collide ...

Deposit power >140W \rightarrow exceeds quench limit of the superconducting magnets. Luminosity limit found at L≈2.3 x 10²⁷ cm⁻² s⁻¹ (≅50W into magnet)



Quench Risk Mitigation with Orbit Bumps

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Orbit bumps are used to move the secondary beam losses to a less vulnerable location in order to reduce risk of quench.



Careful setup of bumps in beginning of the run to achieve desired loss displacement.

Technique operationally used in ATLAS/CMS since 2015. Allowed record luminosity of L > 6 x 10²⁷ cm⁻² s⁻¹ in 2018.

BFPP Mitigation around ALICE & LHCb

Due to different optics around ALICE and LHCb, bump technique does not work.

<u>ALICE</u>

- Peak luminosity limited by detector saturation to 1 x 10²⁷ cm⁻² s⁻¹.
- Bump to distribute losses over two cells.



<u>LHCb</u>

- No mitigation implemented.
- 75ns bunch scheme provides many more collisions in LHCb.
- Peak luminosity levelled **1 x 10²⁷cm⁻²s⁻¹**



BFPP Mitigation around ALICE & LHCb – LS2 Upgrade

Due to different optics around ALICE and LHCb, bump technique does not work.

ALICE

- Currently implementing upgrade
- Will allow to go to ~7 x 10²⁷cm⁻²s⁻¹
- Installation of **collimator in the empty cryostat** location + orbit bump.



<u>LHCb</u>

- No mitigation foreseen.
- 75ns bunch scheme provides many more collisions in LHCb.
- Peak luminosity levelled **1 x 10²⁷cm⁻²s⁻¹**



More about secondary beams & their treatment discussed in lecture by F. Cerutti







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Accelerator Cycle (Fill)

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Injector cycles (e.g. PS or SPS) are analogous except: collisions \rightarrow extraction

Filling Pattern: Production of Beam in the Injectors



Filling Pattern: design \rightarrow 100ns \rightarrow 75ns



LHC Pb-Pb Bunch Intensities



Screenshot from 2018 operation: bunch intensities at top energy just before collisions

- Injectors provided intensities far above the design.
- Typical structure:
- Along bunch train, due to losses at the SPS injection plateau.
- Along the beam, similar losses in the LHC.
- Max. total number of bunches per beam: 733



Intensity and Emittance Evolution

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Beam intensity decay **dominated by burn-off** (losses from production of collisions)

IBS counteracts radiation damping in horizontal plane

In vertical, IBS is negligible → rad. damping leads to shrinkage

Bunch length similar behavior to horizontal emittance

Typical Luminosity Evolution in 2018

Each experiment has individual requirements: max. Luminosity, β^* , crossing-angle, ... \rightarrow Separated machine setup per IP, luminosity levelling, *luminosity sharing*

ATLAS & CMS:

- $\beta^*=0.5$ m, $\theta_c=170\mu$ rad
- Short levelling period
- Record: 6.1 x 10²⁷cm⁻²s⁻¹ peak luminosity

ALICE:

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- $\beta^* = 0.5 \text{m}, \theta_c = 60 \mu \text{rad}$
- Levelled to design saturation level most of the time in physics.
- Upgrade to ~7 x 10²⁷cm⁻²s⁻¹ in LS2.

LHCb:

- β^* = 1.5m, $\theta_c = 250 \mu$ rad
- Also levelled to design value



LHC **Pb-Pb design luminosity** was chosen to be the detector saturation value of the ALICE experiment.



Most of HL-LHC performance demonstrated!

	Pb-Pb (Design)	Pb-Pb (2018 achieved)	"HL-LHC" Pb-Pb (after LS2)	Upgrade Status
Energy [TeV]	7 Z	6.37 Z	7 Z	••• Magnet training
$oldsymbol{eta}^*$ at IP (1/2/5,8) [m]	(0.5, -)	(0.5, 1.5)	(0.5, 1.5)	
Emittance [μ m]	1.5	~2	1.65	
Bunch Intensity [10 ⁸ ions]	0.7	2.2	1.8	
No. Bunches	592	733	1232	SPS RF
Bunch Spacing	100ns	100ns → 75ns	50ns	(slip-stacking)
Peak Luminosity at IP1/2/5/8 [10 ²⁷ cm ⁻² s ⁻¹]	-/1/1/-	6.1/1/6.1/1	?/7/7/?	Uumi levelling
Company in LUCh (not considered in detail yet)				

Green values reached & exceeded LHC design

Some collisions in LHCb (not considered in detail yet)

Delivered Luminosity: Pb-Pb

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LHC design goal of 1nb⁻¹ in Pb-Pb luminosity already exceeded.



Future performance estimate from 2021: 3 nb⁻¹/run → 12 nb⁻¹ in 4 more Pb-Pb runs





LHC has operated in 5 different modes, but was designed only for 2:

- Design: p-p, Pb-Pb
- Upgrade: p-Pb, Xe-Xe (pilot run), Pb81+ (MD in July)

Few hours runs with new particle types showed that the LHC is highly flexible and well under control.

Demonstrating Flexibility

COLLISION MODE UPGRADES





PROTON-LEAD

Storing and Colliding Different Species

Revolution time and RF frequency depend on particle's mass *m*, charge *Q=Ze*:

$$T(p_p, m, Z) = \frac{C}{c} \sqrt{1 + \left(\frac{mc}{Zp_p}\right)^2} \qquad \qquad f_{RF} = \frac{h_{RF}}{T(p_p, m, Z)}$$

where harmonic number h_{RF} = 35640 in LHC

Relation between momenta is fixed by two-in-one magnet design: $p_{Pb} = Zp_p \rightarrow T_p \neq T_{Pb} \rightarrow f_{RF,p} \neq f_{RF,Pb}$ But in order for bunches to meet repeatedly and create collisions we need: $T_p = T_{Pb} \rightarrow f_{RF,p} = f_{RF,Pb}$

→ Use length of closed orbit C to compensate for speed difference. Done by adjusting RF frequency → moving to (slightly) off-momentum orbit

$$T(p_p, m, Z) = \frac{C}{c} \sqrt{1 + \left(\frac{mc}{Zp_p}\right)^2} (1 + \eta \delta)$$

 \rightarrow Pb is slower, need smaller orbit length \rightarrow move inward, $\delta < 0$

 \rightarrow Protons are faster, need longer orbit length \rightarrow move outward, $\delta > 0$

Horizontal offset given by dispersion:

$$\delta = \frac{p - Zp_p}{Zp_p} \quad \begin{array}{l} \mbox{Fractional} \\ \mbox{momentum} \\ \mbox{momentum} \\ \mbox{difference} \\ \mbox{momentum} \\ \mbox{difference} \\ \mbox{momentum} \\ \mbox{q} = \frac{1}{\gamma_T} - \frac{1}{\gamma} \quad \begin{array}{l} \mbox{Phase-slip factor,} \\ \mbox{p}_T = 55.8 \mbox{ for} \\ \mbox{LHC optics} \\ \end{array}$$

 $\Delta x = D_x(s)\delta$

Momentum Offset required through Ramp CERN

Minimize needed aperture \rightarrow take average f_{RF} of both beams and share required momentum offset:

$$\delta_p = -\delta_{Pb} = \frac{c^2 \gamma_T^2}{4p_p^2} \left(\frac{m_{Pb}^2}{Z^2} - m_p^2\right)$$

Horizontal offset given by dispersion:

$$\Delta x = D_x(s)\delta$$





Revolution frequencies must be equal for collisions at top energy. Lower limit on beam energy for p-Pb collisions, E=2.7 Z TeV. **RF** frequencies must be unequal for injection, ramp!

Un-equal Frequency Injection and Ramp

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Both beams circulate on the central orbit, but with un-equal frequencies.

- \rightarrow Arrive at different times in the IP **missing synchronization for collisions** in every turn.
- → At injection and during energy ramp beams are always **kept separated** to avoid collisions anyway.

When being accelerated, the speeds of the two species approach each other.



RF frequency program during p-Pb energy ramp

Top Energy: Cogging and Collisions

At top energy (min. 2.7 Z TeV):

- Equalize revolution frequencies for collisions \rightarrow move beams to off-momentum orbit.
- **Cogging**: RF re-phasing to re-establish synchronization of bunch arrival times in IP (see video).
- Squeeze and Collide



History and Performance of p-Pb Collisions at LHC

Long considered desirable by experiments but never included in LHC baseline design.

2005: First estimates
2011: Preparation of LHC + feasibility test
2012: Physics case document + Pilot-run (one night)
2013: 1st full physics runs
2016: 2nd run with multiple collision conditions

	ATLAS/CMS	ALICE	LHCb
2016	190 nb ⁻¹	40 nb⁻¹	30 nb ⁻¹
Total	222 nb ⁻¹	72 nb ⁻¹	35 nb ⁻¹

Future performance estimate: ~700 nb⁻¹/run (ATLAS/CMS) ~350 nb⁻¹/run (ALICE levelled)





UNFORESEEN OPERATIONAL MODES

Xe-Xe Collisions

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- Lighter ions are not part of the present HL-LHC baseline.
 - Potential for higher nucleon-nucleon luminosities (smaller el.mag. cross-sections)
- 17h of low-intensity running with Xe beams in 2017.
 - Demonstrated the feasibility to operate with other species.
 - Great physics outcome fed the interest in lighter ions for HL-LHC era





M. Schaumann - Heavy-Ions in the LHC, JAS'2019, Dubna, Russia

Partially Stripped Ions

- The Gamma Factory initiative proposes to use partially stripped ion (PSI) beams as drivers of a new type, high intensity photon source.
- Initial beam tests with PSI beams have been executed in the SPS in 2017/18.
- In 2018 the LHC injected, accelerated and stored lead ions with one remaining electron (208Pb81+) for the first time.

²⁰⁸Pb⁸¹⁺



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Physics Beyond Colliders

Partially Stripped Ions

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A few Pb81+ bunches circulated at 6.5 Z TeV with **beam lifetimes of ~40 hours**.

Worst collimation cleaning efficiency ever observed. Introduces dominant limit of the beam intensity.



Electrons are stripped off at first interaction with collimators leading to a change of rigidity outside acceptance:

Image BSR

0.5-[u] >

-0.5-

-1+ -1

Loss

maps

18:52:00

19:07:00

2h

UTC time

18:07:00

18:22:00

18:37:00

-0.8

Synchrotron Light Monitor

X [mm] - Energy : 6499 - bunch : 1781

4%

 \rightarrow Pb82+ lost in cell 11R7.

Losses at FT

17:37:00

17:22:00

17:52:00

0.04

0.02

0.01

0.0

27:07:00

10.03 FT

Take home message ...

The LHC is highly flexible: has operated in 5 modes but was designed for 2 Design: p-p, Pb-Pb

Upgrade: p-Pb, Xe-Xe, Pb⁸¹⁺

extraordinary injector performance

optimizations between & during runs

Rapid switching between modes

The LHC Heavy-lon performance is much higher than originally foreseen.

"first 10-year" Pb-Pb luminosity goal of 1nb⁻¹ has been exceeded

demonstrated "HL-LHC" peak luminosity performance Control of heavy-ion beam losses, like collimation & BFPP, is critical, complicated and may surprise.

Heavy ions will come back to the LHC end of 2021 after the injector and LHC hardware upgrades with the "HL-LHC" configuration.





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Everything clear! Hmm



In general an ion is described by

charge *Qe* (Lorenz-Invariant or rest) mass *m* nucleon number ("mass number") *A*.

Mainly collide **fully-stripped ions**, bare nuclei $\rightarrow Q = Z$ (charge or proton number)

in LHC we use ²⁰⁸ Pb ⁸²⁺ with
Z = 82
A = 208

$$\begin{split} m_{208\text{-Pb-82+}} &= 207.976652071 \text{u} - 82 m_e \\ &= (193.729 - 82 \times 0.000511) \text{ GeV / } \text{c}^2 \\ &= 193.687 \text{ GeV / } \text{c}^2 \end{split}$$

N.B. $208m_p = 195.161 \text{ GeV} / c^2$ is a poor approximation! For this species the binding energy of the 82 electrons < 1 MeV.

1u = 931.49410242(28) MeV



Critical difference between RHIC and LHC

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The Idea of a Gamma Factory



1.) Resonant absorption of the laser photons by the Partially Stripped Ion (PSI) beam.

2.) Followed by a spontaneous atomictransition emissions of secondary photons.

LASER photon strongly boosted by $(2\gamma_{rel})^2 \rightarrow$ For LHC energy, photon energy exceeds those reachable for FEL at high light intensity.



- Technique to obtain **effective 50/50ns bunch spacing within Pb trains**. Builds together with LEIR intensity upgrade the new LIU baseline option.
- The SPS is filled with 2 "super-batches" of 6 x 4-bunch-PS-batches with a bunch spacing of 100ns.
- The 2 super-batches are captured by two independently controlled 200MHz cavity systems.



- a) Decelerate first super-batch, accelerate second super-batch.
- b) Batches are allowed to slip until they interleave.
- c) Bring back to same energy.
- a) Recapture at an average RF frequency.



LHCb interaction point is displaced by **15 buckets (=37.5ns)** with respect to symmetry point.

In order to have a collision in LHCb a long-range (LR) beam-beam encounter is required at a distance of 37.5ns or 11.25m away from the symmetry point.

Long-range beam-beam encounters occur at **s** = **n x** ½ **bunch spacing**:

25ns bunch spacing \rightarrow LR @ 12.5ns, 25ns, **37.5ns** ... \rightarrow **collisions in LHCb** 50ns bunch spacing \rightarrow LR @ 25ns, 50ns ... \rightarrow need to displace a train of bunches to create collisions **75ns bunch spacing** \rightarrow LR @ **37.5ns**, 75ns ... \rightarrow **collisions in LHCb** 100ns bunch spacing \rightarrow LR @ 50ns, 100ns ... \rightarrow need to displace a train of bunches to create collisions





The **Beam Loss Monitor (BLM) System** measures secondary particles from beam losses all around LHC circumference.





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Notations – Energy of ions/nuclei and nucleons

Energy and momentum are related via the square of the 4-momentum vector, $\mathbf{P} = (E / c, \mathbf{p}),$

$$P^2 = \frac{E^2}{c^2} - p^2 = m^2 c^2$$

Nucleus of• charge Ze• (rest) mass m• nucleon number A

where *m* is the Lorentz-invariant mass (rest mass) of the nucleus.

Traditionally, in low-energy ion accelerators, the kinetic energy per nucleon is quoted in parameter lists:

$$E_{kin} = rac{\sqrt{p^2 c^2 + m^2 c^4} - mc^2}{A} pprox rac{E}{A}$$
 at high energy

but this quantity does not appear in any equation of motion!

At LHC (highly relativistic case) we use:

$$E \approx pc = 7.0 Z \text{ TeV} = 2.76 A \text{ TeV} = 574 \text{ TeV}$$

Energy per charge,
relation to proton energy Energy per nucleon Energy of the particle

Derive Center-of-Mass Equations for Collisions of two Species

$$(P_{1} + P_{2})^{2} = (E_{1} + E_{2})^{2}/c^{2} - (\vec{p}_{1} + \vec{p}_{2})^{2}$$

$$= E_{1}^{2}/c^{2} + E_{2}^{2}/c^{2} + 2E_{1}E_{2}/c^{4} - \vec{p}_{1}^{2} - \vec{p}_{2}^{2} - 2p_{1}p_{2}\cos\alpha$$

$$= 4p_{1}p_{2}$$

$$4p_{p}^{2}Z_{1}Z_{2}$$

$$\sqrt{(P_1 + P_2)^2} = \sqrt{s} = 2p_p^2 \sqrt{Z_1 Z_2}$$
$$\sqrt{s_{NN}} = 2p_p^2 \sqrt{\frac{Z_1 Z_2}{A_1 A_2}}$$

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Center-of-Mass Energy

Center-of-Mass Energy per nucleon

The total luminosity in 1 experiment

is the **sum over all colliding individual bunches** of the 2 beams:

$$\mathcal{L} = \sum_{(i,j)\in\text{coll.pairs}}^{k_b} \frac{N_{1,i}N_{2,j}f_{\text{rev}}\sqrt{\gamma^2 - 1}}{2\pi\beta^*\sqrt{\epsilon_{x,1,i} + \epsilon_{x,2,j}}\sqrt{\epsilon_{y,1,i} + \epsilon_{y,2,j}}}$$

Integrated Luminosity Prediction per Pb-Pb run

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For a 24-day run, with 3 experiments at $\beta^*=0.5$ m, assuming (pessimistically) an operational efficiency of 50% and average luminosity of 3E27 cm⁻² s⁻¹, the total luminosity is

 $L_{int,annual} = (50\%)(3.0 \times 10^{27} \text{ cm}^{-2}\text{s}^{-1})(24 \text{ day}) \approx 3.1 \text{ nb}^{-1}$ (c.f. target of 2.85 nb⁻¹)

→ 12 nb⁻¹ in the 4 Pb-Pb runs foreseen after LS2

Integrated Luminosity Prediction per p-Pb run

• Assuming

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- a turnaround time of 2.5 h (optimistic!)
- operational efficiency of 50%,
- and optimal fill length of 6.1 h,
- The total luminosity in 1 month of p-Pb running is estimated to
 - 714 nb⁻¹ for ATLAS/CMS
 - 346 nb⁻¹ for ALICE

Getting protons into the LHC

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Linac

PSB

PS

SPS

LHC

The CERN accelerator complex Complexe des accélérateurs du CERN



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Steady increase of luminosity/fill

Increasing Levelling targets (ATLAS/CMS/LHCb) Levelling time (after solving ALICE beam size problem)

Source: http://lpc.web.cern.ch/

Levelling "a la carte"

Under certain conditions and depending on the experiments request, it is desirable to adapt the luminosity dynamically with beams in collision – **luminosity levelling**





Levelling by beam offset

Levelling by crossing angle

Levelling by β^* (= beam size at IP)





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Intra-Beam Scattering

Intra-Beam Scattering Growth Rates

$$\alpha_{\mathrm{IBS},s} = \left\langle A_{\mathrm{p}} \frac{r_{h}^{2}}{r_{p}^{2}} f(a,b,q) \right\rangle$$

$$\alpha_{\mathrm{IBS},x} = \left\langle A_{\mathrm{p}} \left[f\left(\frac{1}{a}, \frac{b}{a}, \frac{q}{a}\right) + \frac{D_{x}^{2}\sigma_{h}^{2}}{\sigma_{x}^{2}} f(a,b,q) \right] \right\rangle$$

$$\alpha_{\mathrm{IBS},y} = \left\langle A_{\mathrm{p}} \left[f\left(\frac{1}{a}, \frac{b}{a}, \frac{q}{a}\right) + \frac{D_{y}^{2}\sigma_{h}^{2}}{\sigma_{x}^{2}} f(a,b,q) \right] \right\rangle$$
Complicated Integral,
to be evaluated
numerically at each
element of lattice
$$f(a,b,q) = 8\pi \int_{0}^{1} \left\{ 2\ln \left[\frac{q}{2} \left(\frac{1}{P} + \frac{1}{Q} \right) \right] - 0.577 \dots \right\} \frac{1 - 3u^{2}}{PQ} du$$

$$A_{\mathrm{p}} = \frac{2r_{0}^{2}cN_{b}}{64\pi^{2}\beta_{\mathrm{rel}}^{3}\gamma^{4}\epsilon_{x}\epsilon_{y}\sigma_{s}\sigma_{p}}$$
Dynamic change with
beam parameters
$$\frac{1}{\sigma_{h}^{2}} = \frac{1}{\sigma_{p}^{2}} + \frac{D_{x}^{2}}{\sigma_{x}^{2}} + \frac{D_{y}^{2}}{\sigma_{y}^{2}}$$

$$g^{2} = a^{2} + (1 - a^{2})u^{2}$$

Radiation Damping

CÉRN

The average energy loss into synchrotron radiation in a circular accelerator leads to damping of the transverse and longitudinal **emittances** like $\int_{1}^{1} dt = \int_{1}^{2} r dt dt$

$$A_{i} = A_{0,i}e^{-\alpha_{\text{rad},i}t}$$
, where $i = x, y, s_{i}$



Note: 1.) Independ of beam parameters.
 2.) Depend on Energy³, machine size and particle type.

3.) In this approximation, longitudinal damping is twice as fast as transverse: $\alpha_{\text{rad},s} = 2\alpha_{\text{rad},x} = 2\alpha_{\text{rad},y}$.

4.) Rad. damping for Pb 2x faster than for protons: $\alpha_{rad,xy} = 12h$

5.) Fast enough to overcome IBS at full energy and intensity



Data used to estimate future running.

Lighter ions have potential for **significantly higher nucleon-nucleon luminosity**:

- Expect higher bunch charge in the injector chain
- Lower cross sections for ultraperipheral collisions

 $\rightarrow \sigma_{\text{BFPP}} \sim Z^7$, $\sigma_{\text{EMD}} \sim Z^4$

 \rightarrow Slower burn-off and longer fills, more ions left for usable luminosity







Beam Evolution

A particle bunch is characterised by its **number of particles**, $N_b(t)$, and the **emittances**, $\epsilon_{n,i}(t)$, in the three planes (i = x, y, s).



 α are growth rates or inverse lifetimes, describing how fast the corresponding process changes a quantity.

The bunch's evolution is usually obtained by (numerically) solving those differential equations, or by tracking simulations.