

**$\Delta$ -ISOBAR CONTRIBUTION TO THE PION  
PRODUCTION IN THE REACTION  $pp \rightarrow \{pp\}_s \pi^0$**

**Yu.N. Uzikov**

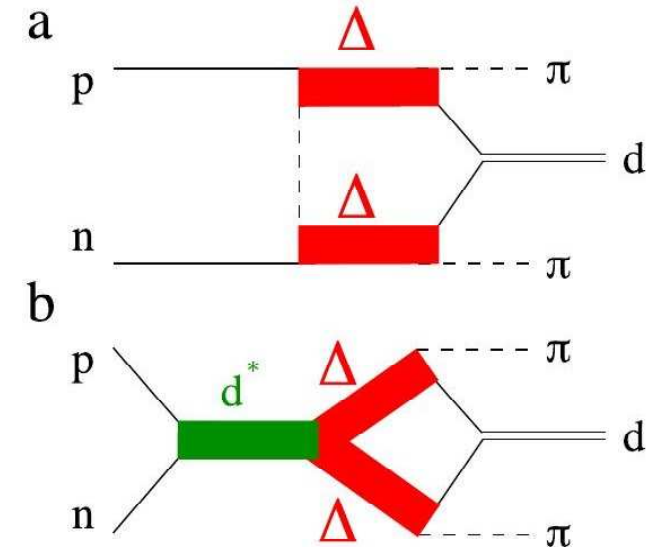
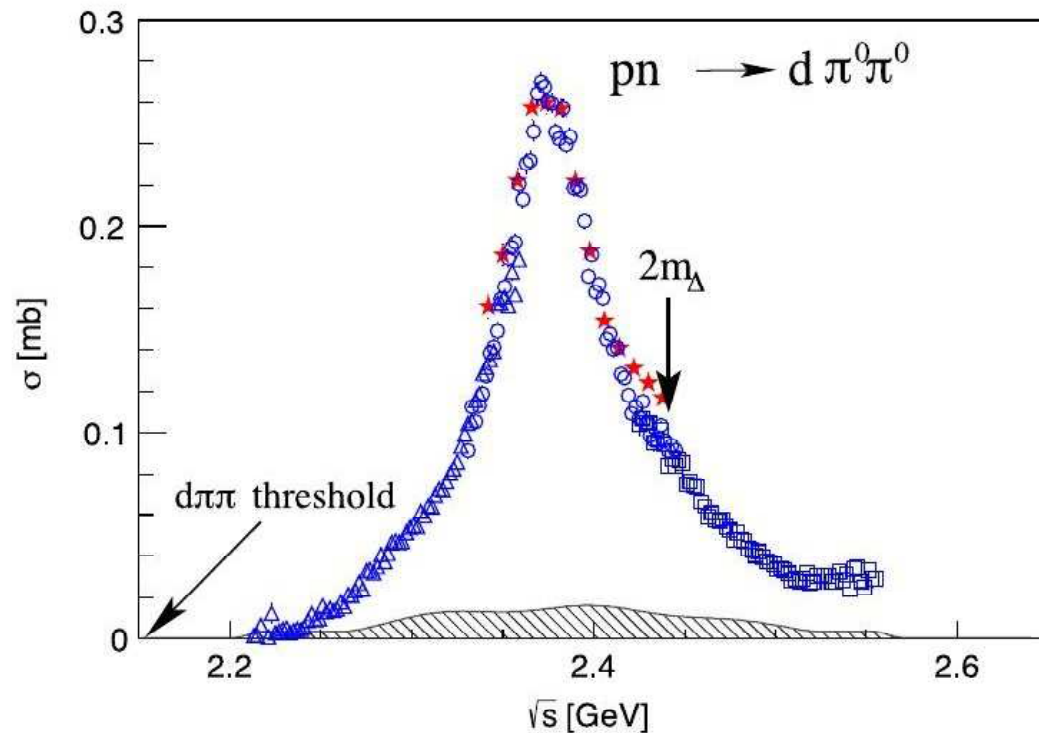
*Joint Institute for Nuclear Research, DLNP, Dubna*

Baldin ISHEPP XXIV Seminar,  
Dubna, Russia, 17-22 September, 2018

- **Renaissance of dibaryon resonance physics in the nonstrange sector (H. Clement, Prog. Part. Nucl. Phys. 93 (2017) 195)**
- **ANKE@COSY data on  $pp \rightarrow \{pp\}_s \pi^0$  at 0.3-0.8 GeV and problems with its theoretical interpretation via the  $\Delta$ -excitation mechanism**

WASA@COSY  $pn \rightarrow d\pi^0\pi^0$ ,  $M = 2380$  MeV,  $\Gamma = 70$  MeV

H. Clement / Progress in Particle and Nuclear Physics 93 (2017) 195–242



*M. Bashkanov et al. PRL 102 (2009) 052301; several others reactions*

**Narrow width:** (i) 6q-models, – Y.-B. Dong, et al. (2016) (hidden colour);  
 (ii) hadron picture,  $\pi N \Delta$  system – A. Gal, H. Garcilazo, PRL 111 (2013) 172301;  $\Delta\Delta$  system – J. Niskanen, PRC 95 (2017) 054002

/Talk by N. Tursunbayev tomorrow/

- Dubna, 1957,  $p + {}^{12}\text{C} \rightarrow d + X$  at 670 MeV,  
D.I. Blokhintsev: fluctons (6q) in nuclei.

- $\Delta(1232)$  in  $pd \rightarrow dp$  at  $\sim 500 - 600$  MeV:

N.S. Craigie, C. Wilkin, (1969) **OPE**; V.M. Kolybasov, N.Ya. Smorodinskya (1973)

L. Kondratyuk, F. Lev, L.Shevchenko (1979-1982) :

$\Delta + B3$ , TRIBARIONS (9q)!

O.Imambekov, Yu.N. U., L.Shevchenko (1988-1989):

$\Delta$ -dominates  $d\sigma/d\Omega$  but does not solve the  $T_{20}$  puzzle!  $\implies$  Spin structure of  $NN \rightarrow N\Delta$  is not well known.

- $\Delta(1232)$  is against of multiquark exotics

- How to suppress the  $\Delta$ -contribution in  $pd$ - and  $pN$ -interactions?

## Motivation

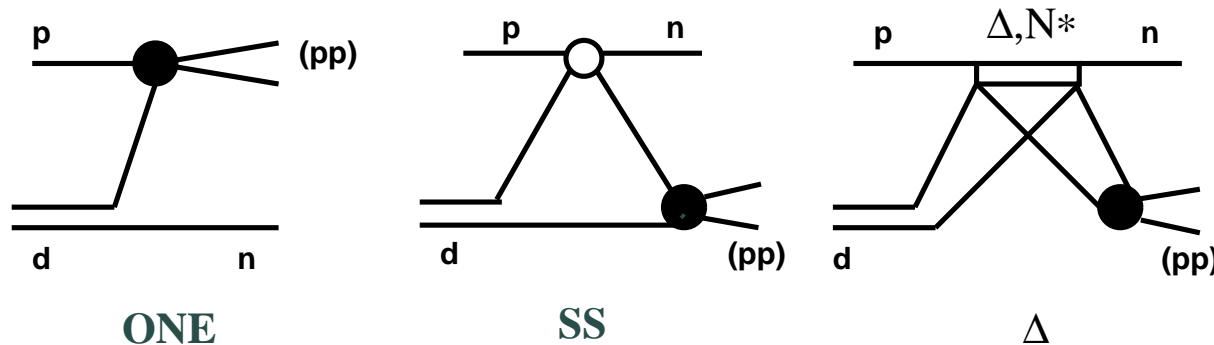
- Reactions with the  $^1S_0$  diproton  $\{pp\}_s$  (i.e.  $E_{pp} < 3$  MeV) at large  $Q$  can give more insight into underlying dynamics due to difference in quantum numbers

deuteron  $\implies (^1S_0)$ pn singlet deuteron or  
 $\implies (^1S_0)$ -diproton,  $\{pp\}_s$

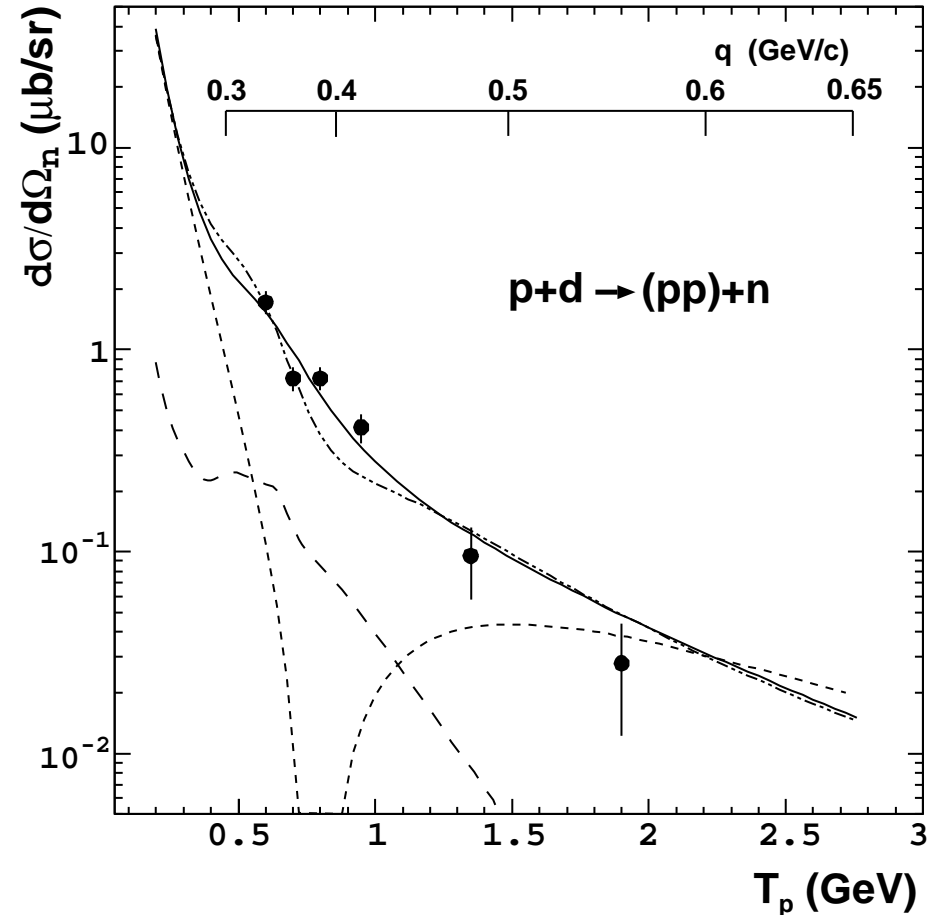
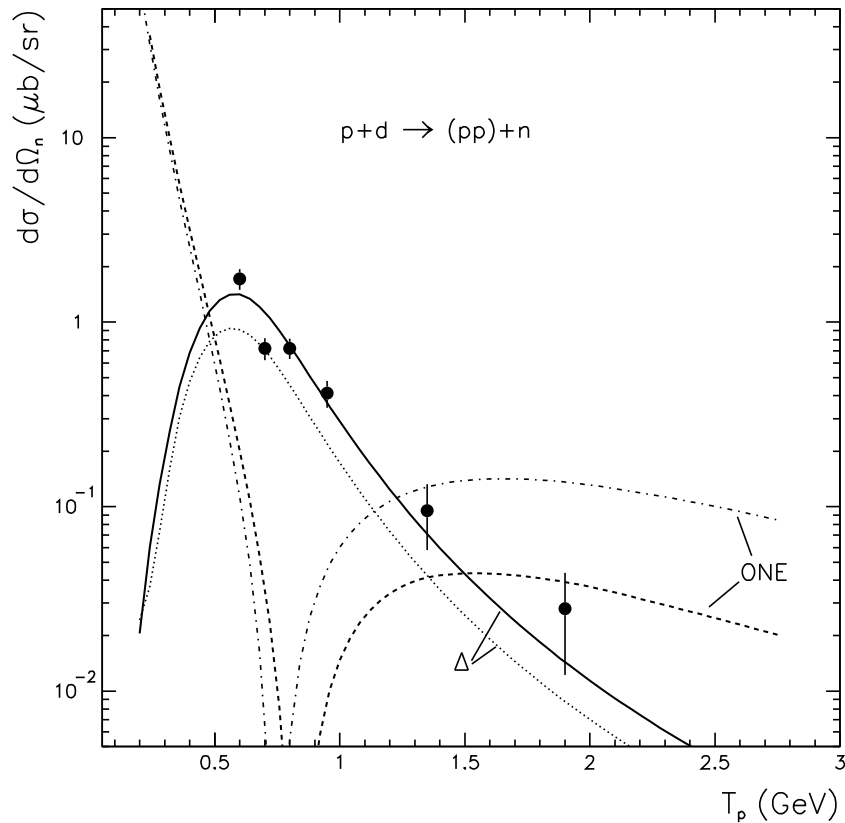
1.  $pd \rightarrow dp \implies p\{NN\}_s \rightarrow dN$  in  $A(p,Nd)B$   
suppression of the  $\Delta$ - and  $N^*$ -excitations as 1 : 9

and  $pd \rightarrow \{pp\}_s n$

**/O.Imambekov , Yu.N.Uzikov, Yad. Fiz. 52 (1990) 1361/**



# ANKE@COSY $pd \rightarrow (pp)_s n$



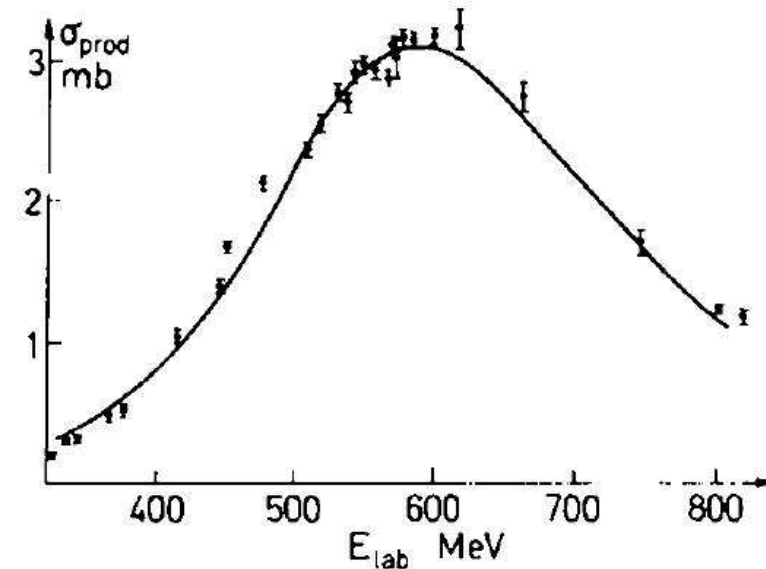
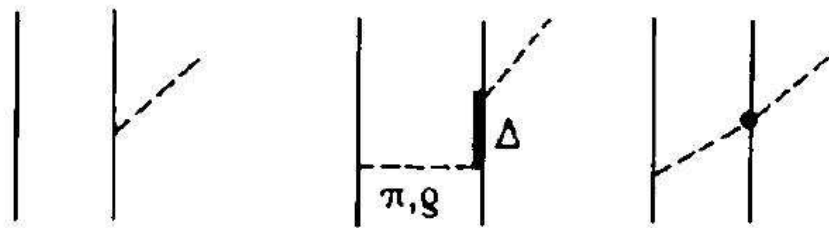
**ONE+ $\Delta$ +SS calculation** (*J.Haidenbauer, Yu.Uzikov, Phys.Lett. B562(2003)227*)

When changing hard  $V_{NN}$  (RSC, Paris) to the soft  $V_{NN}$  (CD Bonn), **ONE decreases** and  **$\Delta$ -increases** providing agreement with the COSY data *V. Komarov et al., Phys. Lett. B553 (2003) 179*.

**$\Delta$  is still large!**

The short range  $V_{NN}$  is rather soft like for the CD Bonn model, but not the RSC and Paris.

$pp \rightarrow d\pi^+$  in the  $\Delta$ -region



J. Niskanen, Phys.Lett. **141B** (1984) 301

But M. Platonova, V. Kukulín, NPA **946** (2016) 117: the  $\Delta$  mechanism alone is not sufficient, dibaryon resonances were introduced:  $^1D_2p$  (2150 MeV,  $\Gamma = 110$  MeV),  $^3F_3d$  (2200-2260 MeV  $\Gamma = 150$  MeV) to get an agreement, including polarizations, PRD **94** (2016)) with  $pp \rightarrow d\pi^+$ .

**Thus, it is important to study another channel:  $pp \rightarrow \{pp\}_s \pi^0$  at similar kinematics**

## 2. $pp \rightarrow d\pi^+$ & $pp \rightarrow \{pp\}_s\pi^0$

$^1S_0$  diproton:  $J^\pi = 0^+$ ,  $T = 1$ ,  $S = 0$ ,  $L = 0$

deuteron:  $J^\pi = 1^+$ ,  $T = 0$ ,  $S = 1$ ,  $L = 0, 2$

- $(-1)^{L+S+T} = -1$  (Pauli principle)

- Spin-parity conservation:

★  $pp \rightarrow d\pi^+$ , odd and even  $L_{pp}$ ,  $S = 1$  and  $S = 0$ ;

$\implies \Delta N$  in S-wave (  $N^*N$  )  $\pi = +1$  - *is allowed*

$\implies \Delta(1232)$  dominates in the  $pp \rightarrow d\pi^+$  at  $\approx 600$  MeV

★  $pp \rightarrow \{pp\}_s\pi^0$  odd  $L_{pp}$ ,  $S = 1$

$\implies \Delta N$  in S-wave (or  $N^*N$ )  $\pi = +1$  - *is forbidden*



## Diproton physics at ANKE-COSY, 2000-2014

$pd \rightarrow \{pp\}_s n$ , hard deuteron breakup 0.5 - 2.0 GeV

$pp \rightarrow \{pp\}_s \pi^0$

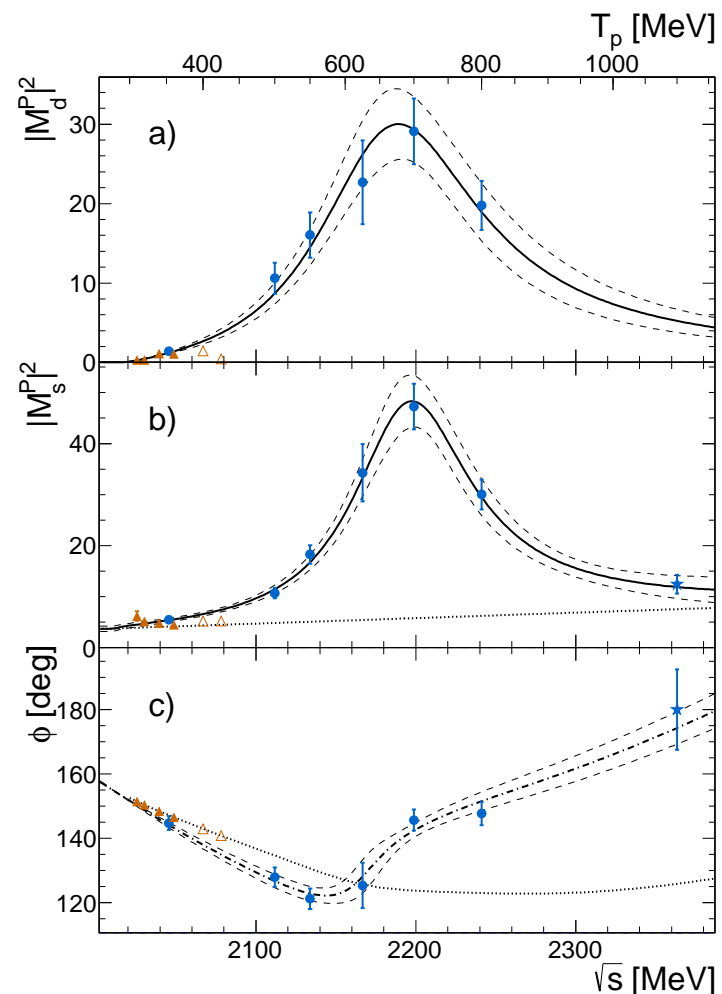
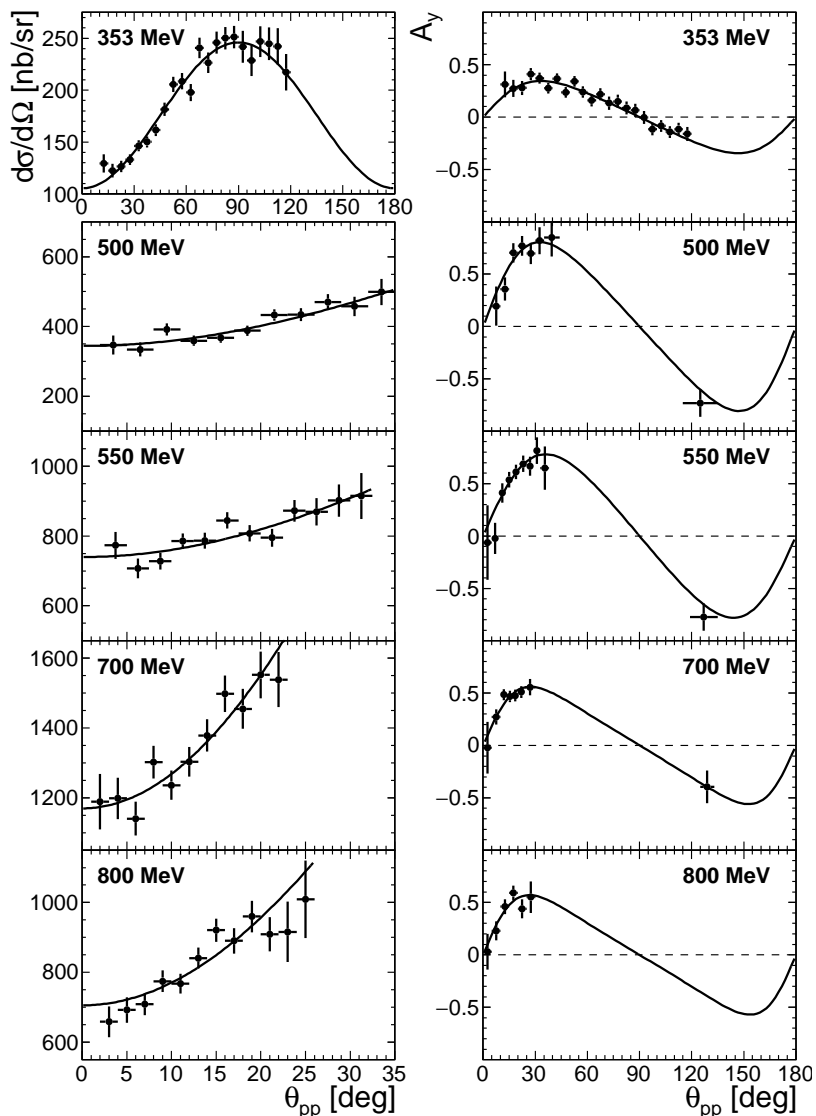
$pp \rightarrow \{pp\}_s \gamma$

$pp \rightarrow \{pp\}_s \pi\pi$

$pn \rightarrow \{pp\}_s \pi^-$ ,  $T_p = 350$  MeV, the contact d-term for ChPT

$dp \rightarrow \{pp\}_s N\pi$ ,  $T_d = 1.6 - 2.3$  GeV  $\pi N = \Delta$ - excitation

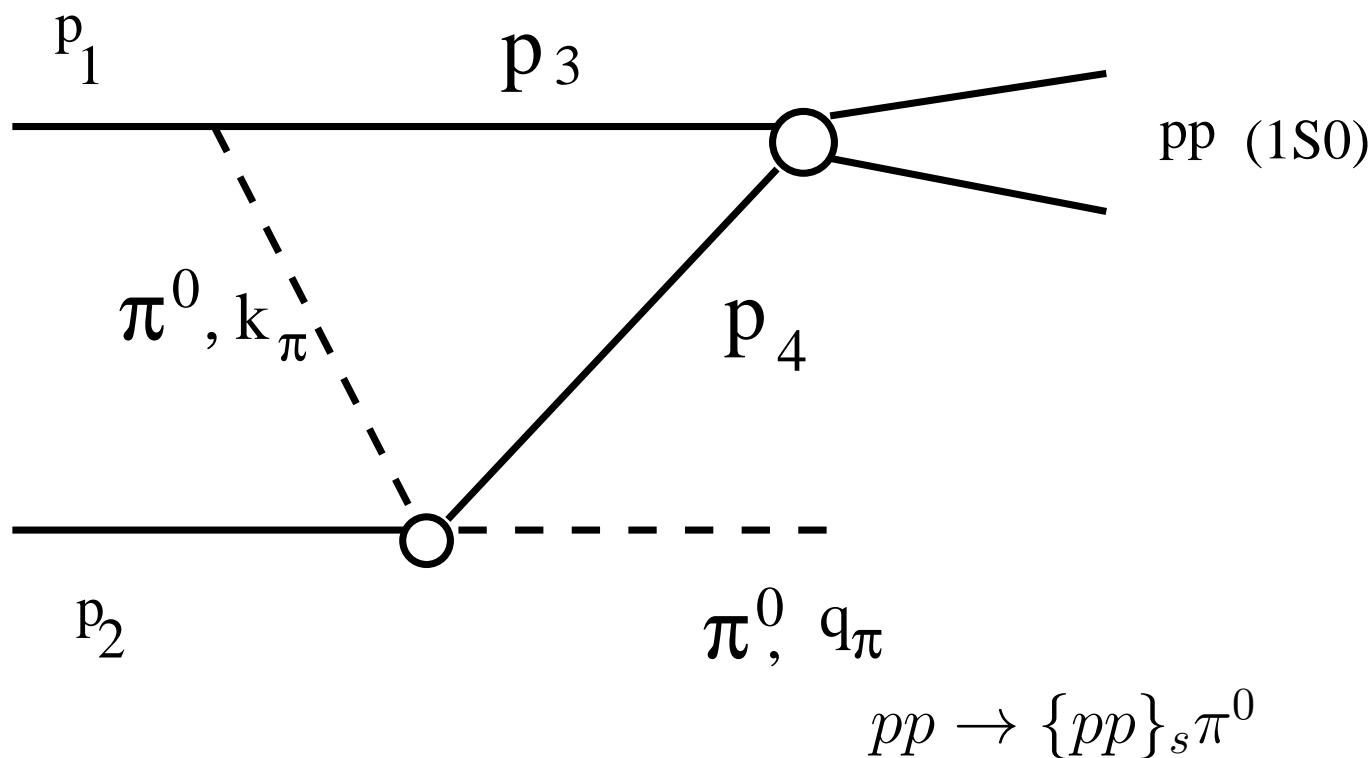
Talk by V. Kurbatov tomorrow on  $pp \rightarrow \{pp\}_s \pi^0$  at 1.5 - 2.8 GeV



**Two  $T = 1$  resonances are found with almost equal masses 2205 MeV:**  
 $J^p = 0^-$  ( ${}^3P_0s$ ),  $J^p = 2^-$  ( ${}^3P_2d$ );  $\Gamma_0 = 95 \pm 9$  MeV  $\Gamma_2 = 170 \pm 32$  MeV;  
 anomalous angular dependence is observed as compared to  $pp \rightarrow d\pi^+$

## The OPE model

The same approach which describes well  $pp \rightarrow d\pi^+$  via  $\Delta$ -mechanism fails in case of  $pp \rightarrow \{pp\}_s \pi^0$  (J.Niskanen, PLB **642** (2006) 34). That's way we start with the OPE



The  $\pi N \rightarrow \pi N$  is taken off the loop integral

How to exclude  $\Delta$  from  $\pi^0 p \rightarrow \pi^0 p$ ?

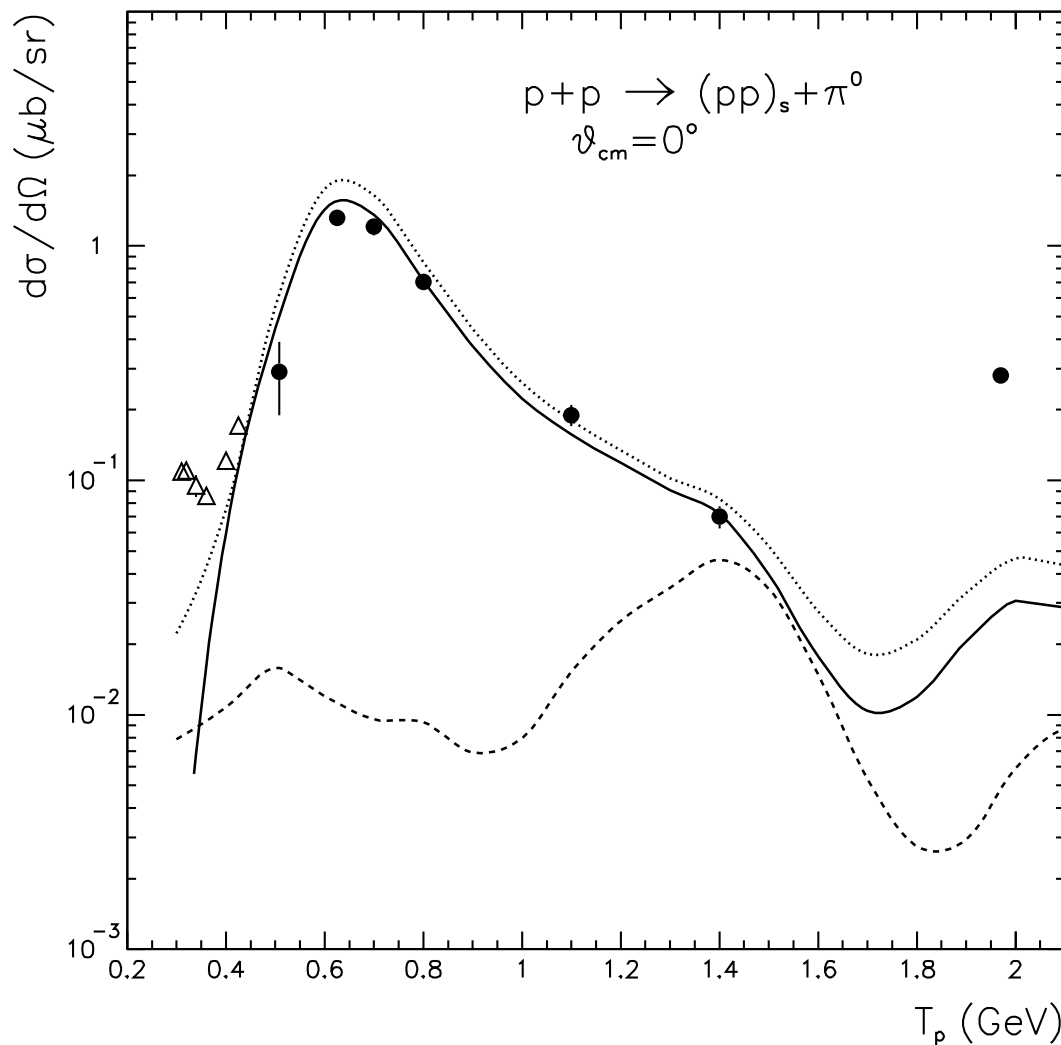
$$\mathbf{A}(\pi^0 \mathbf{p} \rightarrow \pi^0 \mathbf{p}) = \frac{1}{3} \left( \mathbf{a}_{\frac{1}{2}} + 2\mathbf{a}_{\frac{3}{2}} \right), \quad (1)$$

$$\mathbf{d}\sigma(\pi^0 \mathbf{p} \rightarrow \pi^0 \mathbf{p}) = \frac{1}{2} \left\{ \mathbf{d}\sigma(\pi^+ \mathbf{p}) + \mathbf{d}\sigma(\pi^- \mathbf{p}) - \mathbf{d}\sigma(\pi^0 \mathbf{n} \rightarrow \pi^- \mathbf{p}) \right\}, \quad (2)$$

If the amplitude  $a_{\frac{3}{2}}$  is excluded from Eq. (1)

$$\mathbf{d}\tilde{\sigma}(\pi^0 \mathbf{p} \rightarrow \pi^0 \mathbf{p}) = \frac{1}{18} \left\{ 3\mathbf{d}\sigma(\pi^- \mathbf{p}) - \mathbf{d}\sigma(\pi^+ \mathbf{p}) + 3\mathbf{d}\sigma(\pi^0 \mathbf{n} \rightarrow \pi^- \mathbf{p}) \right\}. \quad (3)$$

$pp \rightarrow \{pp\}_s \pi^0$ : The OPE results with (full line) and without (dashed)  $\Delta(1232)$



Normalization factor  $N = \frac{1}{2.5}$

● – COSY data V. Kurbatov et. al, PLB 661 (2008) 33

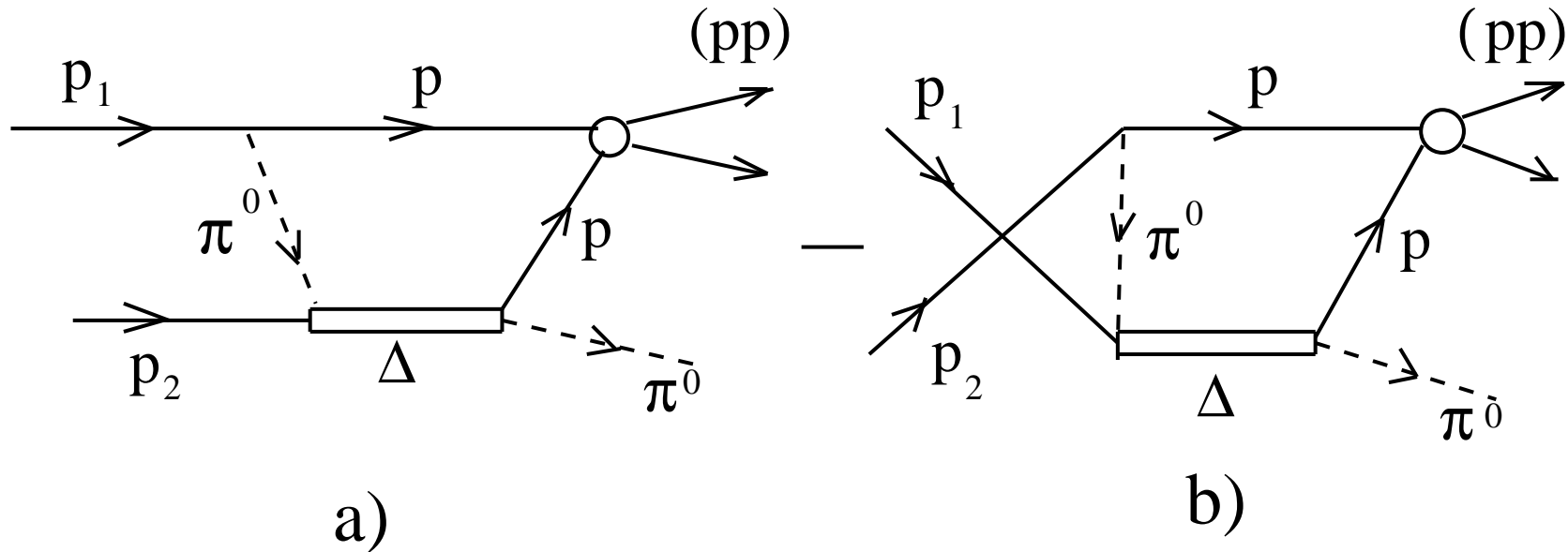
*OPE:  $pp \rightarrow \{pp\}_s \pi^0, pp \rightarrow \{pp\}_s \gamma$*

The OPE mechanism does not allow one to take into account the Pauli principle  $(-1)^{S+T+L} = -1$  because the direct and exchange diagrams are not involved explicitly.

Even  $L$  must be excluded.

An explicit consideration of the  $\Delta$ -isobar is required.

The BOX-diagramm with  $\Delta$  for  $p\pi^0 \rightarrow p\pi^0$



$$A_{\sigma_1\sigma_2}^{dir} = -8m_{\Delta}m_p^2 N_{pp} \left( \frac{f_{\pi NN}}{m_{\pi}} \right) \left( \frac{f_{\pi N\Delta}}{m_{\pi}} \right)^2 \frac{2}{3} \frac{i}{\sqrt{2}} G_{\sigma_1\sigma_2}^{dir} \times$$

$$\times \int \frac{F_{\pi NN}(k_{\pi}^2)}{(m_{\pi}^2 - k_{\pi_a}^2 - i\varepsilon)} \frac{F_{\pi N\Delta}(k_{\pi}^2)}{(m_{\Delta}^2 - k_{\Delta_a}^2 - im_{\Delta}\Gamma)} \frac{\langle \Psi_k^{(-)} | V(^1S_0) | \mathbf{q} \rangle}{(k_{pp}^2 - q^2 + i\varepsilon)} \frac{d^3\vec{q}}{(2\pi)^3} \quad (4)$$

Yu.N. Uzikov, Izv.RAN, Ser.Fiz. 81 (2017) 815 / Bull. Rus. Ac. Sci: Physics, 81

(2017) 739/

## $\pi NN, \pi N\Delta$ -vertices; $\Gamma_\Delta(k)$

$$\langle \pi N_2 | N_1 \rangle = \frac{f_{\pi NN}}{m_\pi} \varphi_1^+ (\boldsymbol{\sigma} \mathbf{Q}) (\boldsymbol{\tau} \Phi_\pi) \varphi_2 2m_N,$$

$$\langle \rho N_2 | N_1 \rangle = \frac{f_{\rho NN}}{m_\rho} \varphi_1^+ ([\boldsymbol{\sigma} \mathbf{Q}] \boldsymbol{\epsilon}_\rho) (\boldsymbol{\tau} \Phi_\rho) \varphi_2 2m_N,$$

$$\langle \pi N | \Delta \rangle = \frac{f_{\pi N\Delta}}{m_\pi} (\Psi_\Delta^+ \mathbf{Q}'_\pi) (\mathbf{T} \Phi_\pi) \varphi \sqrt{2m_N 2m_\Delta},$$

$$\langle \rho N | \Delta \rangle = \frac{f_{\rho N\Delta}}{m_\rho} ([\Psi_\Delta^+ \mathbf{Q}'_\rho] \boldsymbol{\epsilon}_\rho) (\mathbf{T} \Phi_\rho) \varphi \sqrt{2m_N 2m_\Delta},$$

where

$$f_{\pi NN} = 1.00, f_{\pi N\Delta} = 2.15,$$

$$f_{\rho NN} = 6.20, f_{\rho N\Delta} = 13.33.$$

V.F. Dmitriev et al (1987)

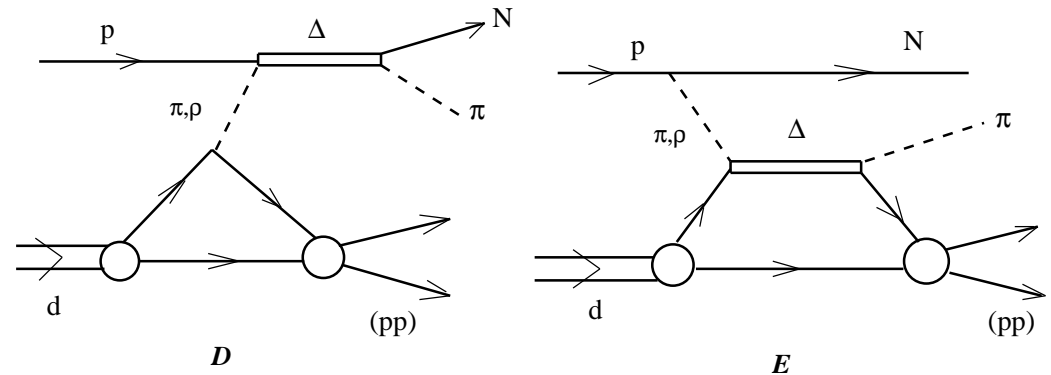
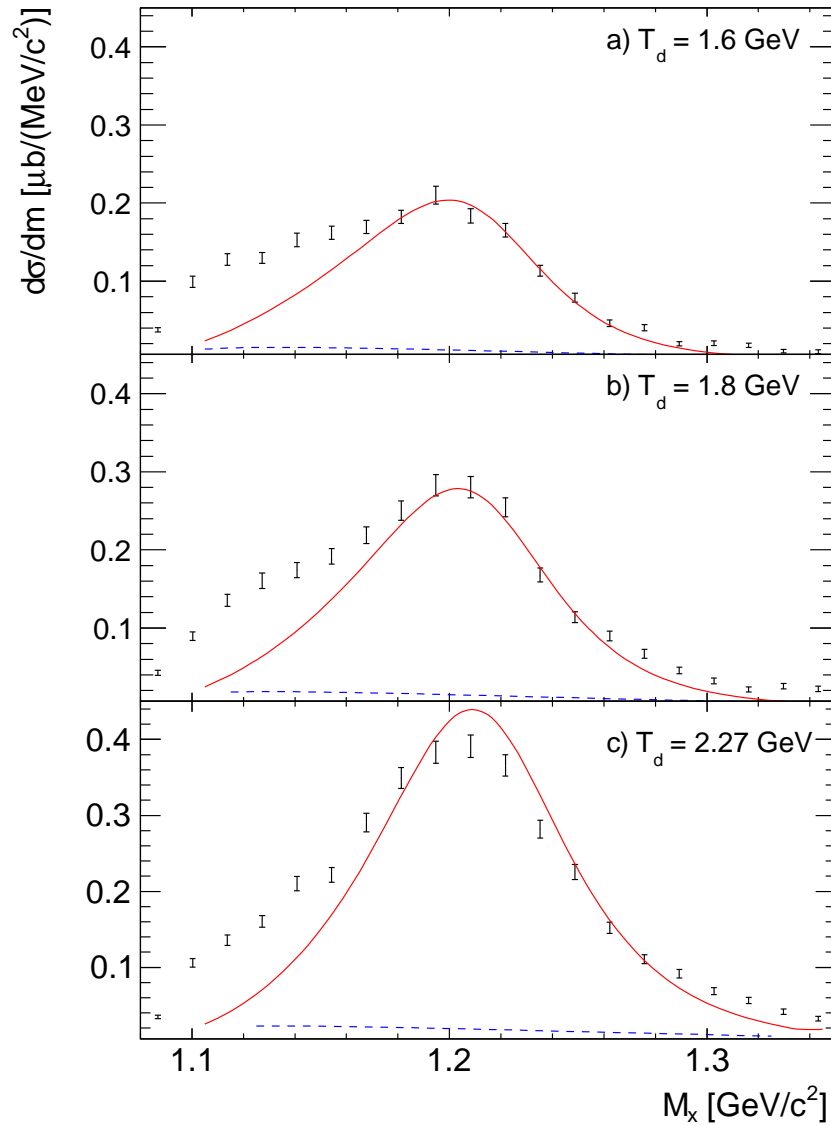
M. Platonova, V. Kukulín, NPA (2016)

$$\Gamma(k) = \Gamma_0 \left( \frac{k_{on}}{k_R} \right)^3 \frac{k_R^2 + \chi^2}{k_{on}^2 + \chi^2}, \quad \Gamma(k) = \Gamma_0 \left( \frac{k_{on}}{k_R} \right)^3 \left( \frac{k_R^2 + \lambda^2}{k_{on}^2 + \lambda^2} \right)^2,$$

$$\mathbf{Z} = \frac{k_R^2 + \chi^2}{k_{on}^2 + \chi^2}, \quad k_{on} = k(s_\Delta, m^2, m_\pi^2); \quad \chi = 0.18 \text{ GeV}, \quad \lambda = 0.3 \text{ GeV}; \quad \sqrt{\mathbf{Z}} \rightarrow \pi N\Delta.$$

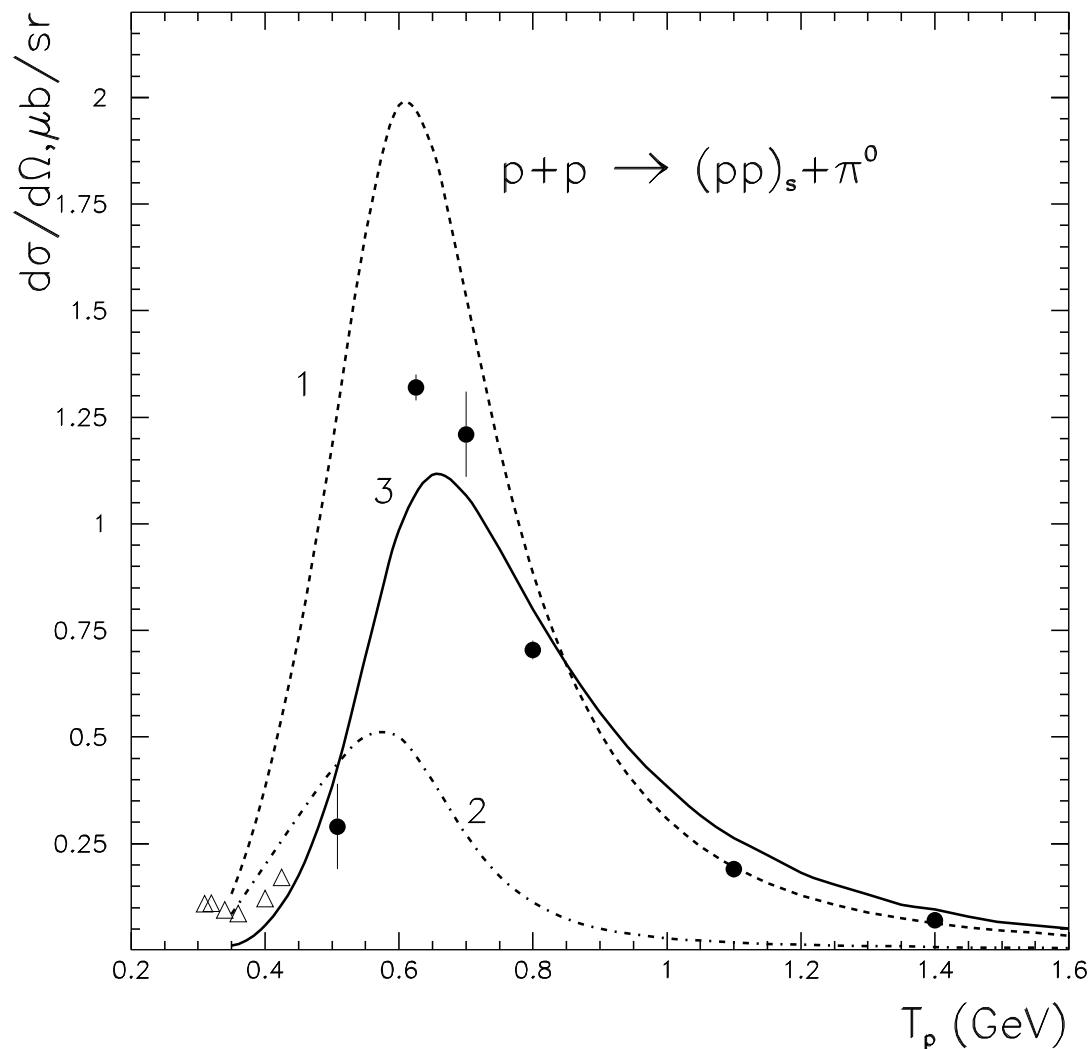


$dp \rightarrow \{pp\}_s \pi N$  Yu.N. U., J.Haidenbauer, C. Wilkin, PoS 93 (2015)



ANKE@COSY data ● – D. Mchedlishvili et al., PRL (2013)  $\lambda_\pi = 0.5$  GeV, and  $T_{22}$

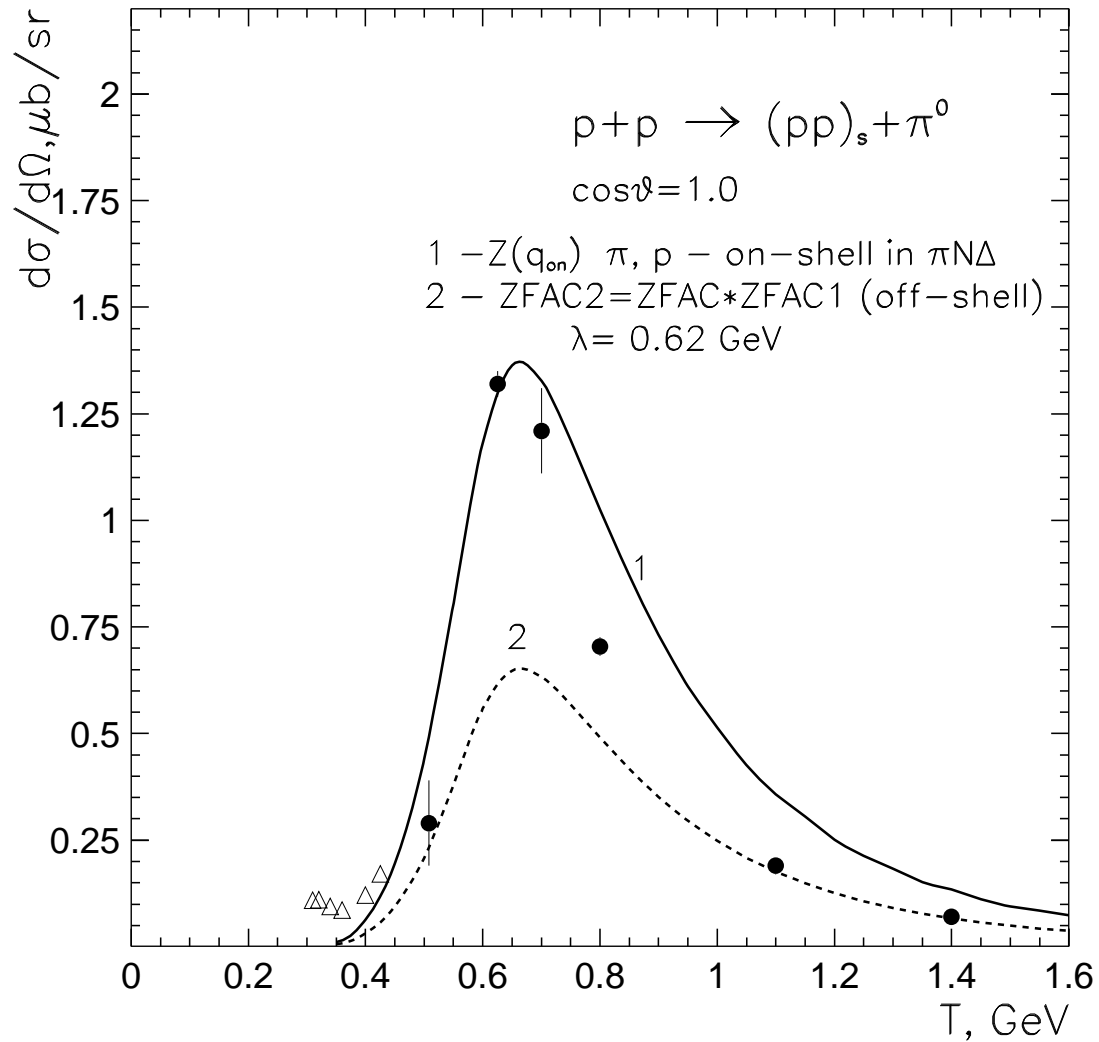
# Z, $\chi = 0.180$ GeV $pp \rightarrow \{pp\}_s \pi^0$



In  $\sqrt{Z}$ -factor in  $\pi N \Delta$   $q = q_{on} = k(s_\Delta, m^2, m_\pi^2)$ : 1- direct, 2-exchange, 3- total;

$$\Gamma(k) = \Gamma_0 \left( \frac{k}{k_R} \right)^3 \frac{k_R^2 + \chi^2}{k^2 + \chi^2} \quad \chi = 0.180 \text{ GeV}, \quad \lambda_\pi = 0.55 \text{ GeV}$$

# Influence of off-shell effects in $\pi N \Delta$ -vertices via $\sqrt{Z}$



Off-shell  $\sqrt{Z}$ -factor in  $\pi N \Delta$ - vertices diminishes  $d\sigma/d\Omega$  (line 2).

Matrix element of  $pp \rightarrow \{pp\}_s \pi^0$ .

$$M = \chi_{\sigma_2}^T(2) \frac{i\sigma_y}{\sqrt{2}} \left( A\vec{\sigma}\hat{p} + B\vec{\sigma}\hat{q} \right) \chi_{\sigma_1}(1) \quad (5)$$

$\vec{p}$  – the proton momentum,  $\vec{q}$  – the pion momentum

$$\frac{d\sigma}{d\Omega} = |A|^2 + |B|^2 + 2\text{Re}AB^* \cos \theta, \quad (6)$$

$$A_y \frac{d\sigma}{d\Omega} = 2\text{Im}AB^* \sin \theta;$$

$$M_{\lambda_1=\frac{1}{2}, \lambda_2=\frac{1}{2}} = -\frac{1}{\sqrt{2}}(A + B \cos \theta) \equiv \Phi_1,$$

$$M_{\lambda_1=\frac{1}{2}, \lambda_2=-\frac{1}{2}} = \frac{1}{\sqrt{2}}B \sin \theta \equiv \Phi_2$$

Jacob, Wick (1959):

$$\begin{aligned} M_{\lambda_1 \lambda_2} &= \sum_J \frac{2J+1}{2} d_{\lambda,0}^J(\theta) \langle 00; JM | JM; l_\pi 0 \rangle \langle JM; LS | JM; \lambda_1 \lambda_2 \rangle A^{(2S+1)} L_J, l_\pi \equiv \\ &\equiv \sum_J \frac{2J+1}{2} d_{\lambda,0}^J(\theta) \Phi_{\lambda_1 \lambda_2}^{(J)}(E), \end{aligned}$$

## The PWA expansion of helicity amplitudes

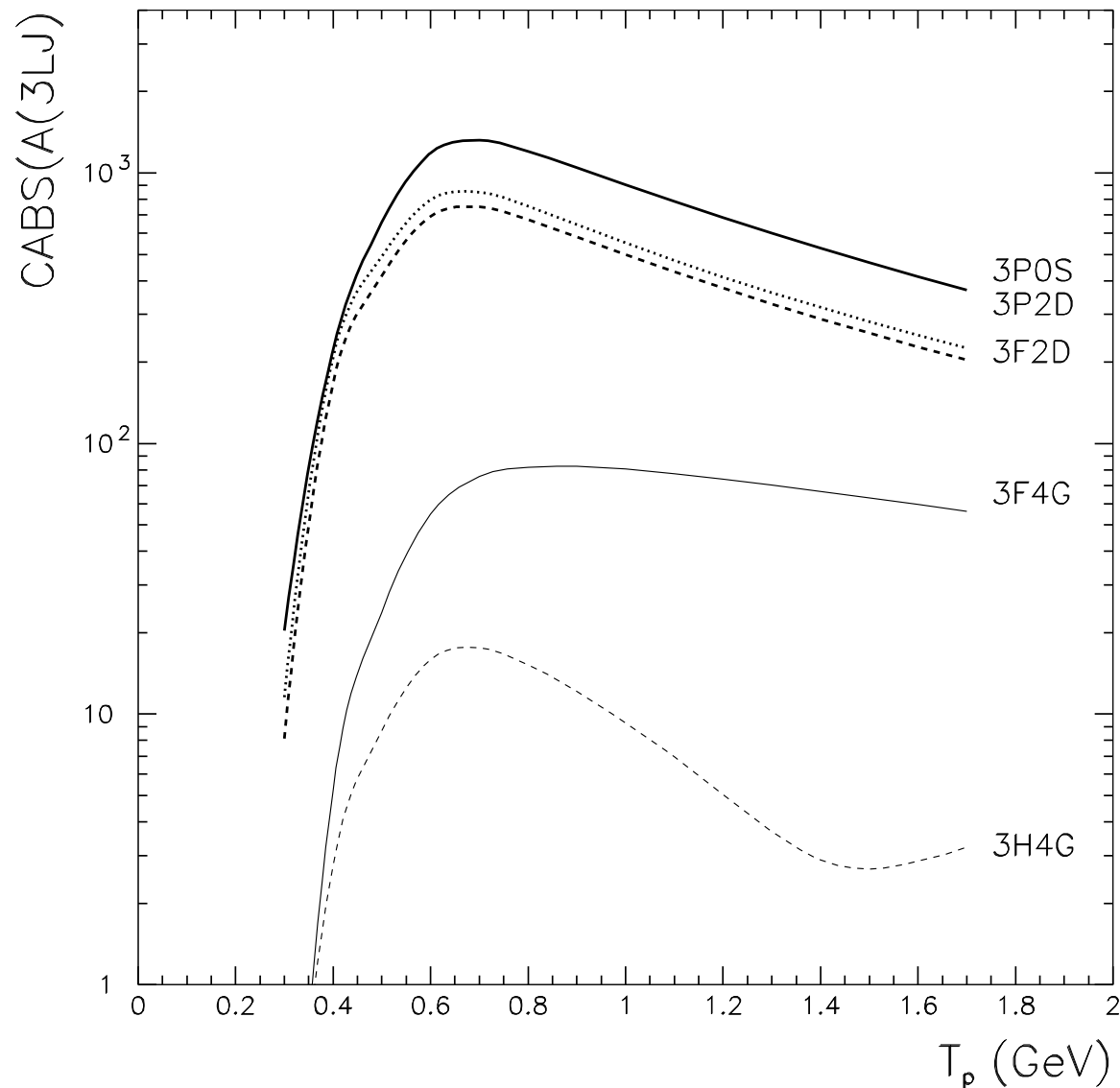
$$\Phi_{\lambda_1 \lambda_2}^{(J)}(E) = \int_0^\pi M_{\lambda_1 \lambda_2}(\theta) d_{\lambda,0}^J(\theta) \sin \theta d\theta. \quad (7)$$

For  $J = 0, 2, 4$ :

$$\begin{aligned} A(^3P_0s) &= -\frac{1}{\sqrt{2}}\Phi_1^{(J=0)}, \\ A(^3P_2d) &= \frac{1}{\sqrt{5}}\Phi_1^{(J=2)} + \sqrt{\frac{3}{10}}\Phi_2^{(J=2)}, \\ A(^3F_2d) &= -\sqrt{\frac{3}{10}}\Phi_1^{(J=2)} + \frac{1}{\sqrt{5}}\Phi_2^{(J=2)}, \\ A(^3F_4g) &= \frac{\sqrt{2}}{3}\Phi_1^{(J=4)} + \frac{1}{3}\sqrt{\frac{5}{2}}\Phi_2^{(J=4)}, \\ A(^3H_4g) &= -\frac{1}{3}\sqrt{\frac{5}{2}}\Phi_1^{(J=4)} + \frac{\sqrt{2}}{3}\Phi_2^{(J=4)}. \end{aligned} \quad (8)$$

For  $J = 0, 2$  coincides with V.Baru et al. (2014))

# PWA for $pp \rightarrow \{pp\}_s \pi^0$ within the $\Delta$ -model: three waves dominate



ANKE fit (V.I. Komarov et al. (2016):  ${}^3P_{0s}$ ,  ${}^3P_{2d}$  are sufficient for  $\frac{d\sigma}{d\Omega}$  and  $A_y(\theta)$ .  
The  $\Delta$ -model:  ${}^3F_{2d}$  cannot be neglected!

*Isospin ratio*  $R = d\sigma(pp \rightarrow \{pp\}_s \pi^0) / d\sigma(pn \rightarrow \{pp\}_s \pi^-)$

To test the mechanism:

$R = d\sigma(pp \rightarrow \{pp\}_s \pi^0) / d\sigma(pn \rightarrow \{pp\}_s \pi^-) = 2$   
for the box diagram with the  $\Delta$ -isobar,

$R = 1/2$  for N-Reggeon exchange

/Yu.N.U., J. Haidenbauer, C. Wilkin, PRC **75** (2007) 014008/

## Summary & Outlook

- So far, indications to exotic (nonstrange) dibaryon resonances usually appear in the region of the  $\Delta$ - or  $\Delta\Delta$ - excitation
- Attempts to suppress the  $\Delta$ -contribution by isospin relations via change  $d \rightarrow \{pp\}_s$ , lead to nontrivial results, e.g. more insight into short-range NN-dynamics in  $pd \rightarrow \{pp\}_s n$
- Well pronounced  $\Delta$ -like resonance structure has been observed in the  $pp \rightarrow \{pp\}_s \pi^0$ , where **S-wave is forbidden in  $\Delta N$  intermediate state**
- In contrast to  $pp \rightarrow d\pi^+$ , the box-diagram with  $\Delta$  completely fails to explain  $\theta$ -dependence  $d\sigma/d\Omega(\theta)$  and  $A_y$  for  $pp \rightarrow \{pp\}_s \pi^0$  and not enough convincing for E-shape of  $d\sigma/d\Omega(0^\circ)$ . Thus, are the  ${}^3P_0s$ ,  ${}^3P_2d$  states **new dibaryons?**...
  - ★  **${}^3F_2d$  would not be neglected in the fit to the data**
  - ★ Necessary to measure  $\frac{d\sigma(pp \rightarrow \{pp\}_s \pi^0)}{d\sigma(pn \rightarrow \{pp\}_s \pi^-)}$



THANK YOU FOR ATTENTION!